

Triaxiality and Wobbling with AGATA

Stein W. Ødegård
University of Oslo



International Workshop on Physics with AGATA
Orsay, 22.03.2004



UNIVERSITY
OF OSLO

Triaxiality and Wobbling with AGATA

- . Triaxiality and Wobbling
- . "Best experimental case" ^{163}Lu
- . Other nuclei in the Lu/Hf region
- . The role of AGATA



**UNIVERSITY
OF OSLO**

Triaxiality and Wobbling

2004



UNIVERSITY
OF OSLO

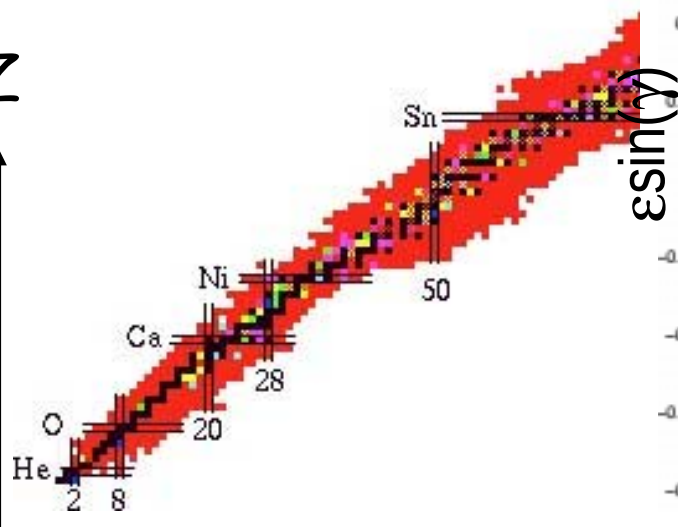
The $A \sim 165$ mass region

$N \sim 94$

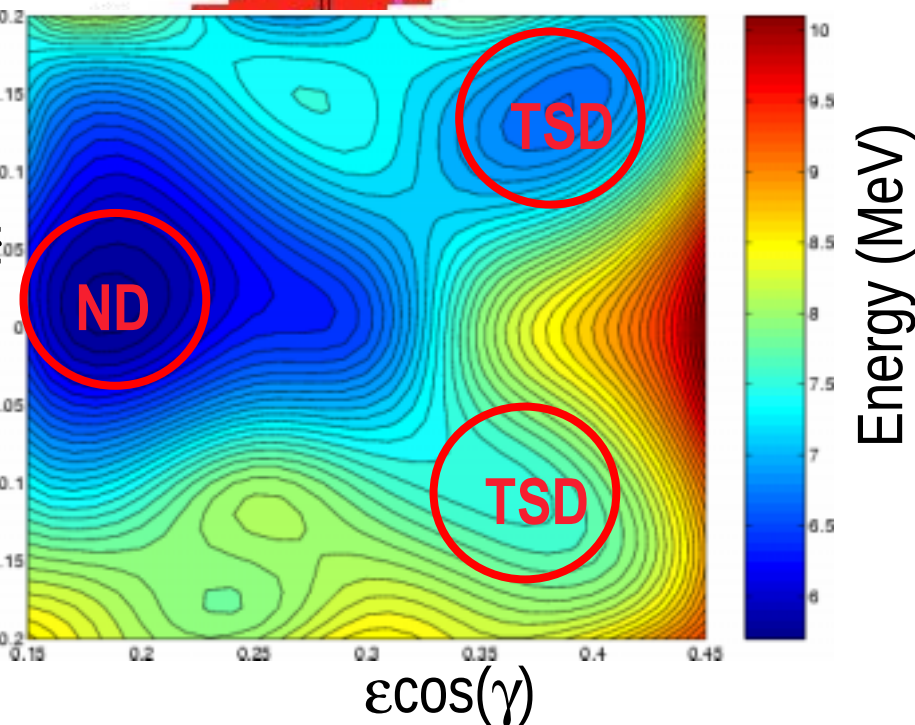
$Z \sim 71$

Total energy surface for ^{163}Lu
 $I=57/2, (\pi, \alpha)=(+, +1/2)$

Z



$\epsilon \sin(\gamma)$



The goal:
To find experimental evidence
for the triaxial deformation



UNIVERSITY
OF OSLO

Signatures of triaxiality

Quasiparticle excitation energy

Relation between signature partner bands

Electromagnetic decay strength between bands

These effects can be caused by other phenomena

Breaking of chiral symmetry

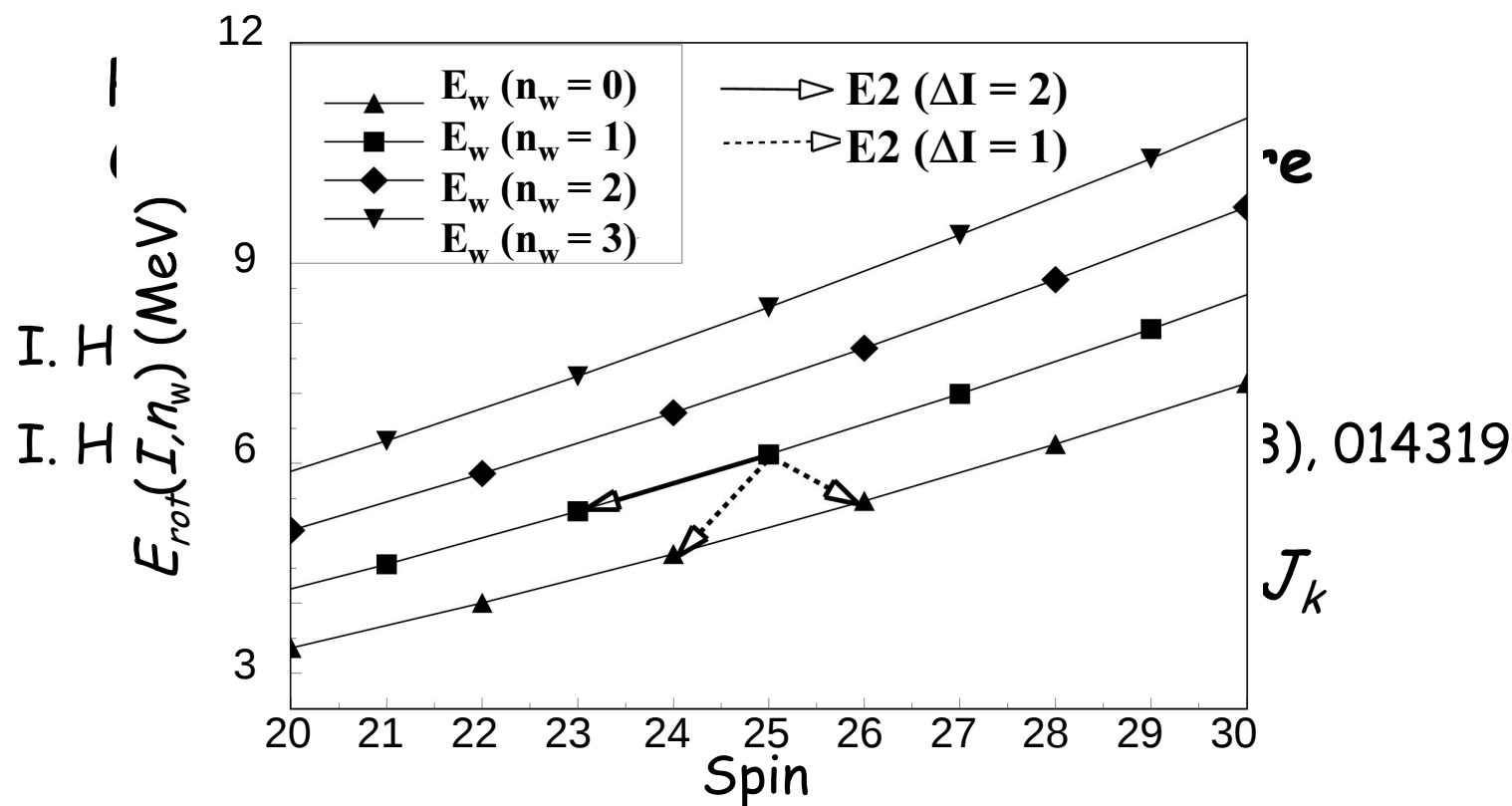
Wobbling excitations

These phenomena are directly related to the triaxiality of the nucleus



UNIVERSITY
OF OSLO

Wobbling in the Odd-even triaxial system



$$E_{rot}(I, n_w) = A_1 I(I+1) + (n_w + \frac{1}{2}) \hbar \omega_w$$



UNIVERSITY
OF OSLO

Wobbling in the Odd-even triaxial system

Particle rotor with:
One **aligned** particle and a **wobbling core**

$$H_{pr} = H_{int} + \sum_{k=1,2,3} A_k R_k^2 \quad , \text{where } \vec{R}_k = (\vec{I} - \vec{j})$$

Assuming $j_1 \approx j$

$$H = A_1 (I_1 - j_1)^2 + A_2 I_2^2 + A_3 I_3^2$$

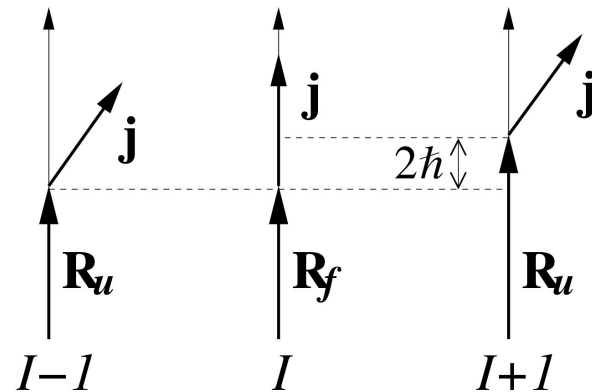
$$E_{rot}(I, n_w) = A_1 I(I+1) + (n_w + \frac{1}{2}) \hbar \omega_w - 2A_1 I_1 j_1 + A_1 j_1^2$$



UNIVERSITY
OF OSLO

Two different ways to couple the particle and core spin

"Crankinglike"





UNIVERSITY
OF OSLO

The signatures of wobbling

Family of rotational bands with similar intrinsic structure and increasing excitation energy.

Observables $J^{(2)}$, i_x , $Q_{\dagger}$, ΔE^*

Characteristic decay pattern between bands, with $\Delta n_w=1$ transitions competing with $\Delta n_w=0$ in-band transitions

Phonon rule:

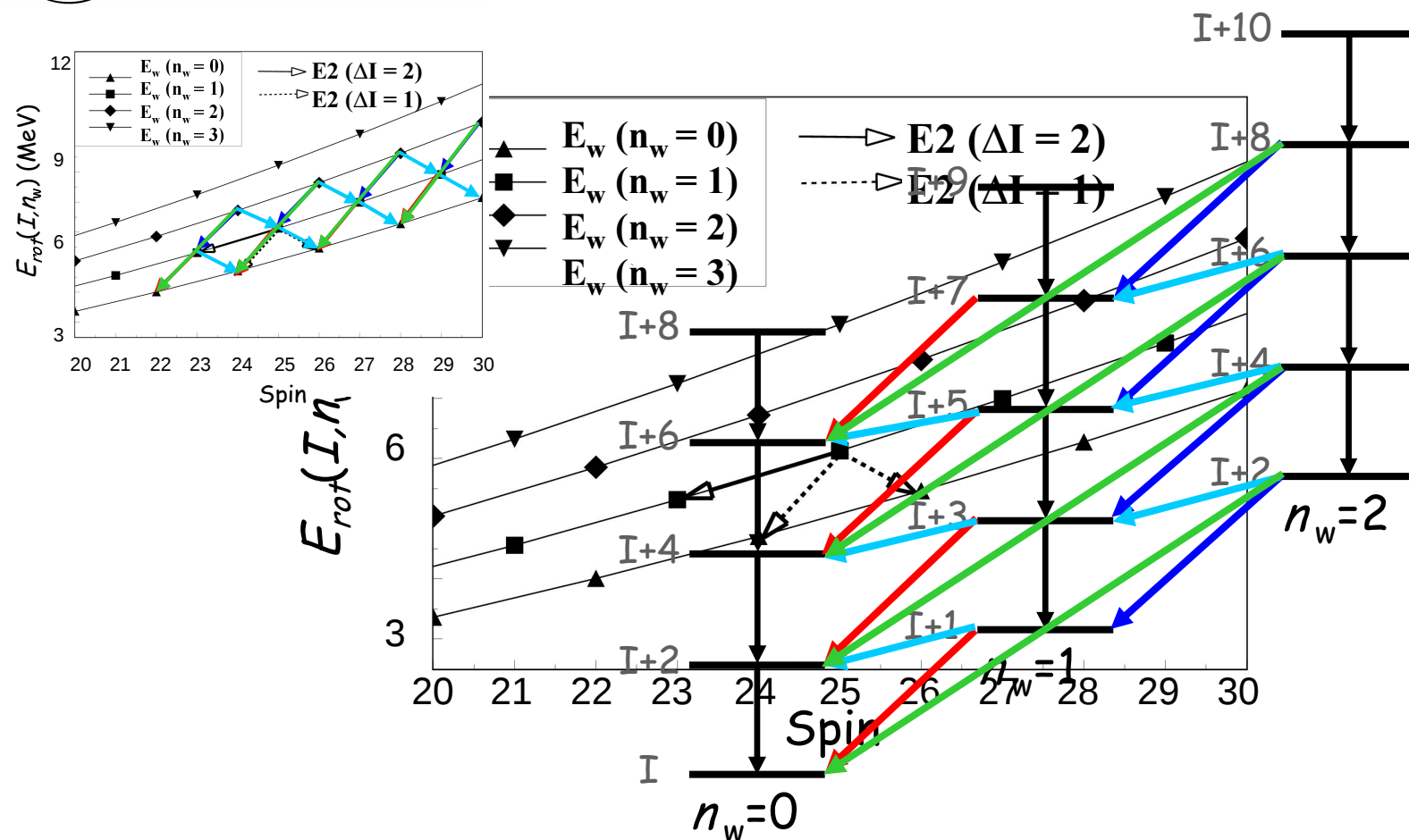
$$B(E2, n_w=2 \rightarrow n_w=1) \approx 2 * B(E2, n_w=1 \rightarrow n_w=0)$$

$$B(E2, n_w=2 \rightarrow n_w=0) \approx 0$$



UNIVERSITY
OF OSLO

The signatures of wobbling





UNIVERSITY
OF OSLO

Information from the connecting transitions

Angular distributions
DCO measurements
Linear Polarisation



Spin and parity
Mixing ratio of E2/M1

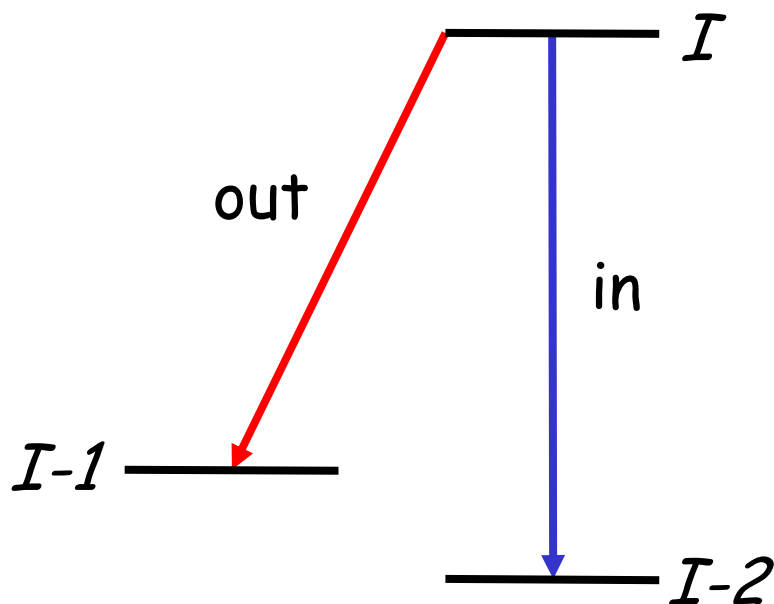


Ratios of reduced
electromagnetic moments

$$B(E2)_{\text{out}}/B(E2)_{\text{in}}$$

and

$$B(M1)/B(E2)_{\text{in}}$$





UNIVERSITY
OF OSLO

Best case: ^{163}Lu



UNIVERSIT
OF OSLO

TSD1

TSD2

TSD3

TSD4

Experimental results in ^{163}Lu
The best "Wobbler"

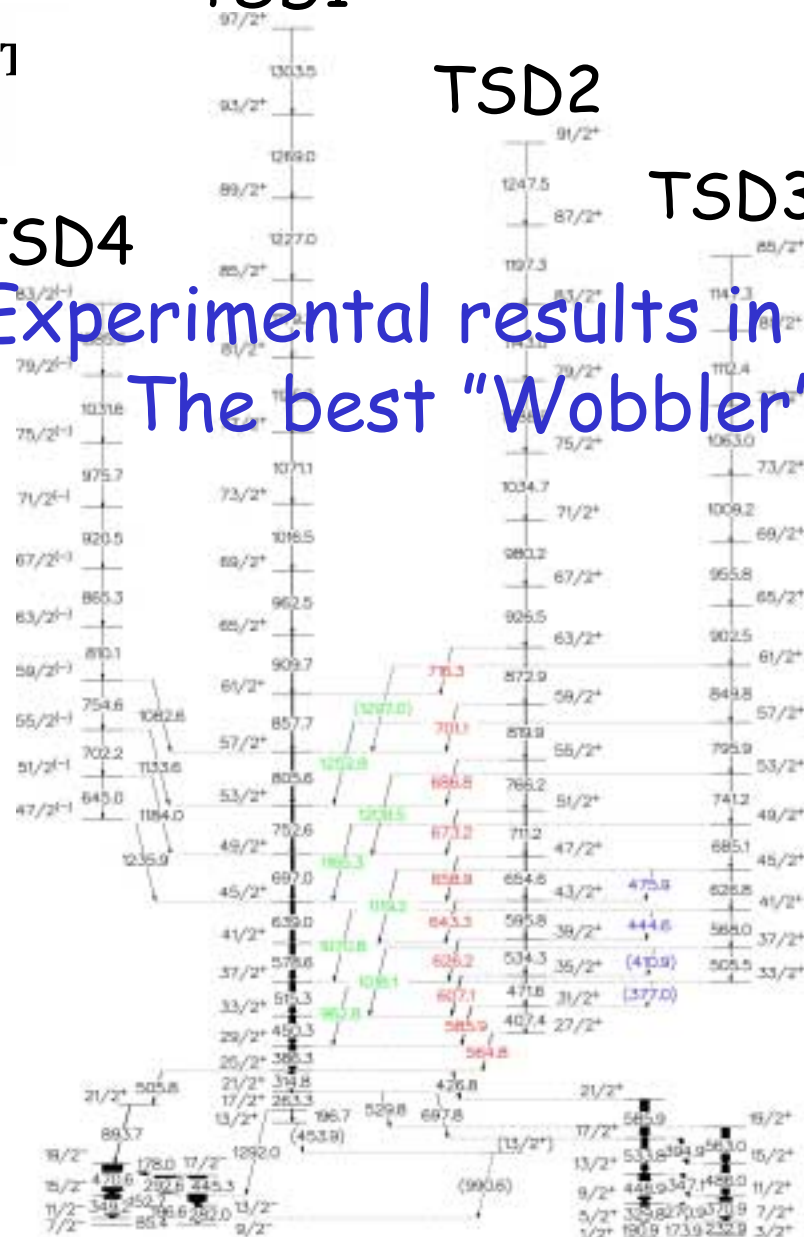
Relative population

TSD1: 10%

TSD2: 3%

TSD3: 1.2%

TSD4: 0.9%



2004

D.R. Jensen et al., Phys. Rev. Lett. **89** (2002), 142503.

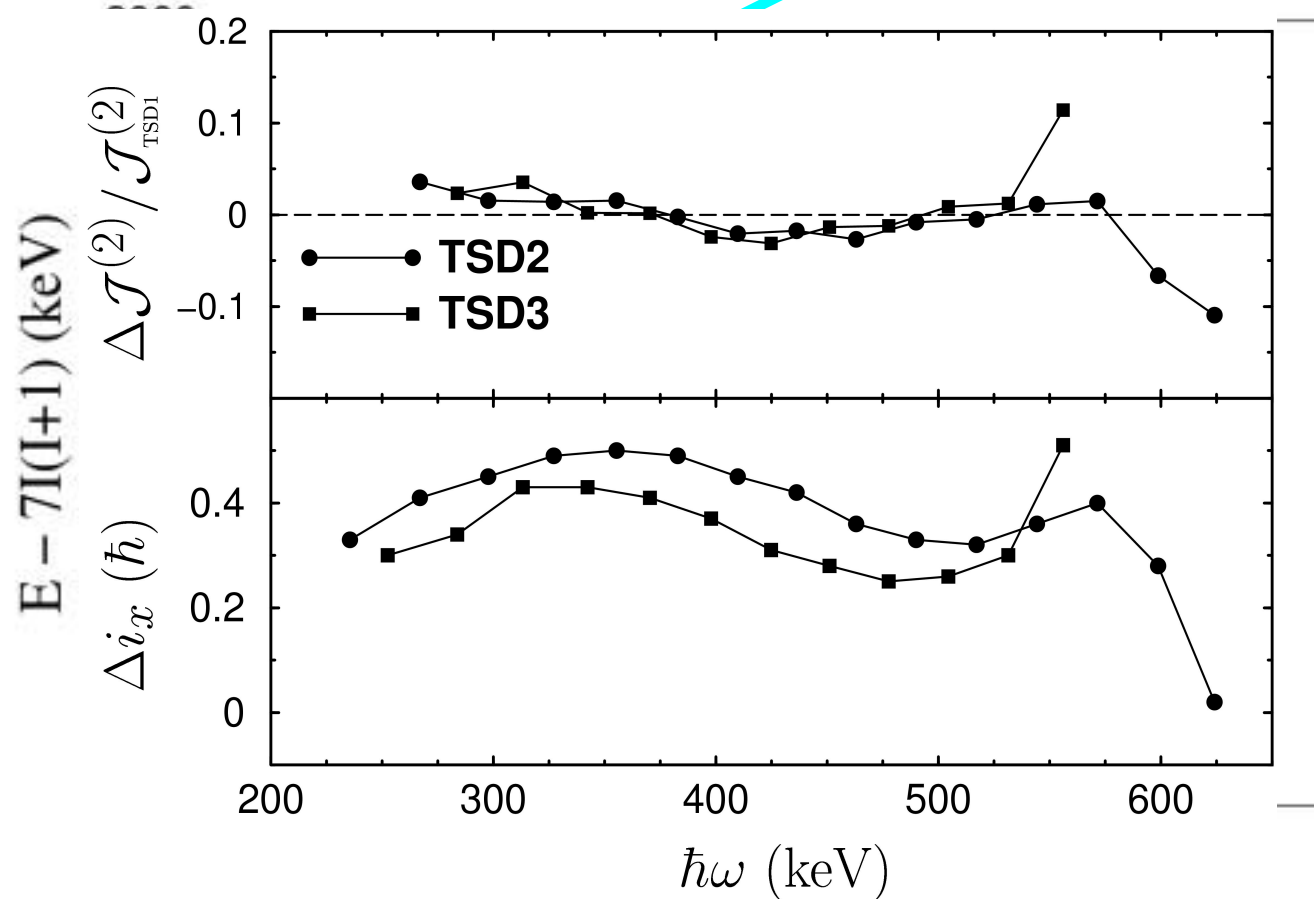




UNIVERSITY
OF OSLO

The family of wobbling bands

Theory: close to rigid moment of inertia D3 relative to TSD1

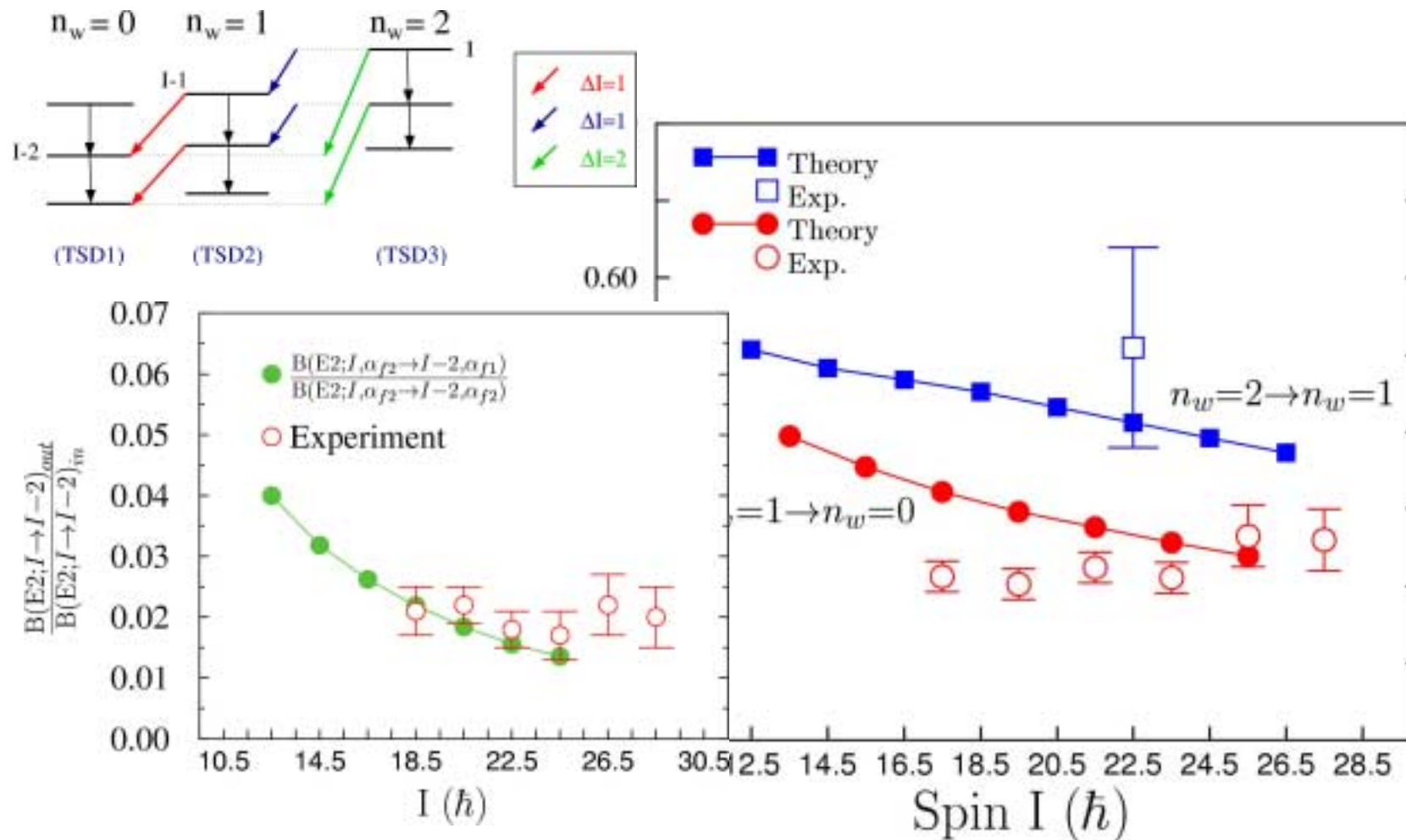


D.R. Jensen et al., Phys. Rev. Lett. **89** (2002), 142503.



UNIVERSITY
OF OSLO

Experiment compared to theory

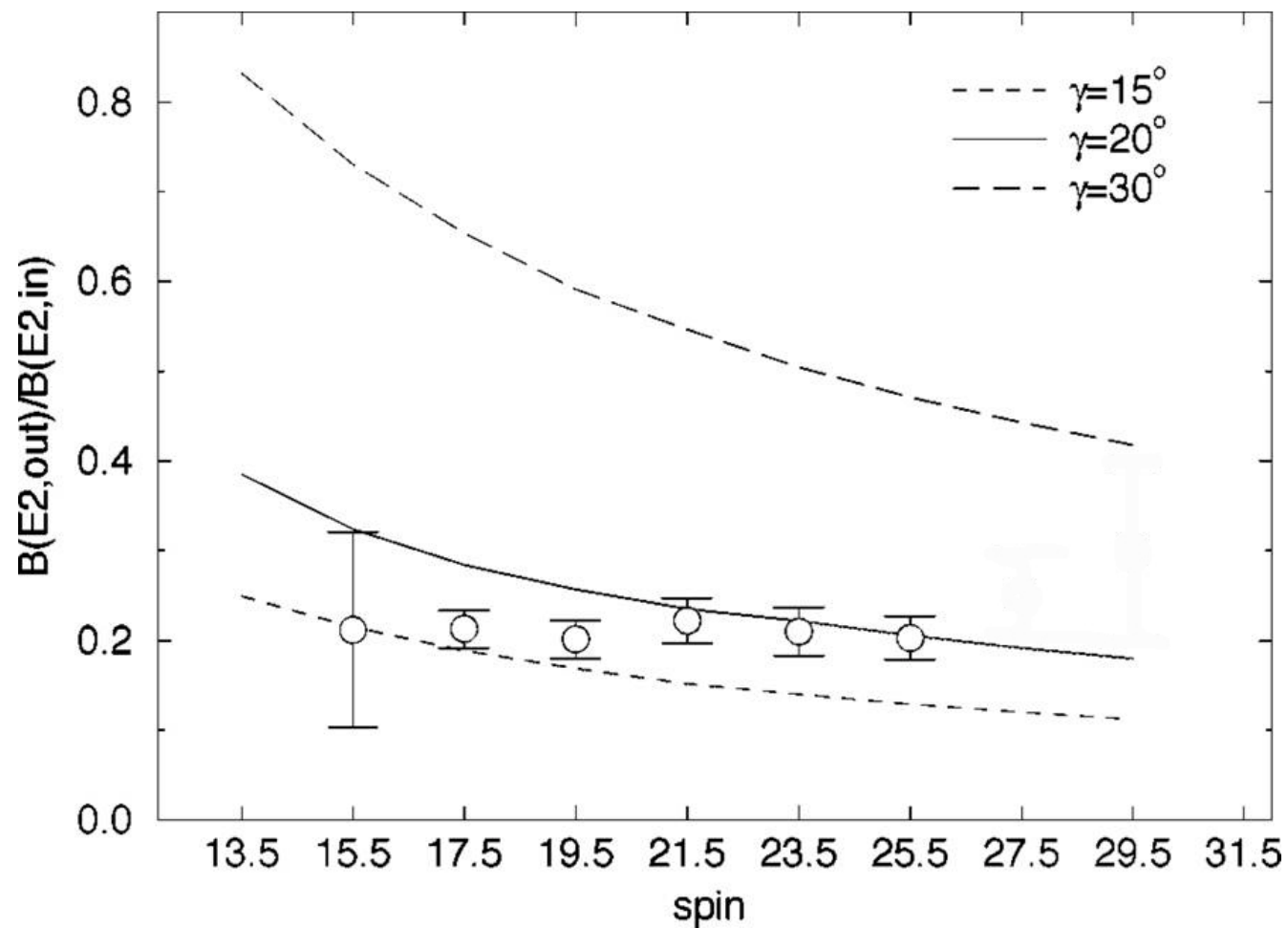


D.R. Jensen et al., Phys. Rev. Lett. **89** (2002), 142503.



UNIVERSITY
OF OSLO

Dependence on γ



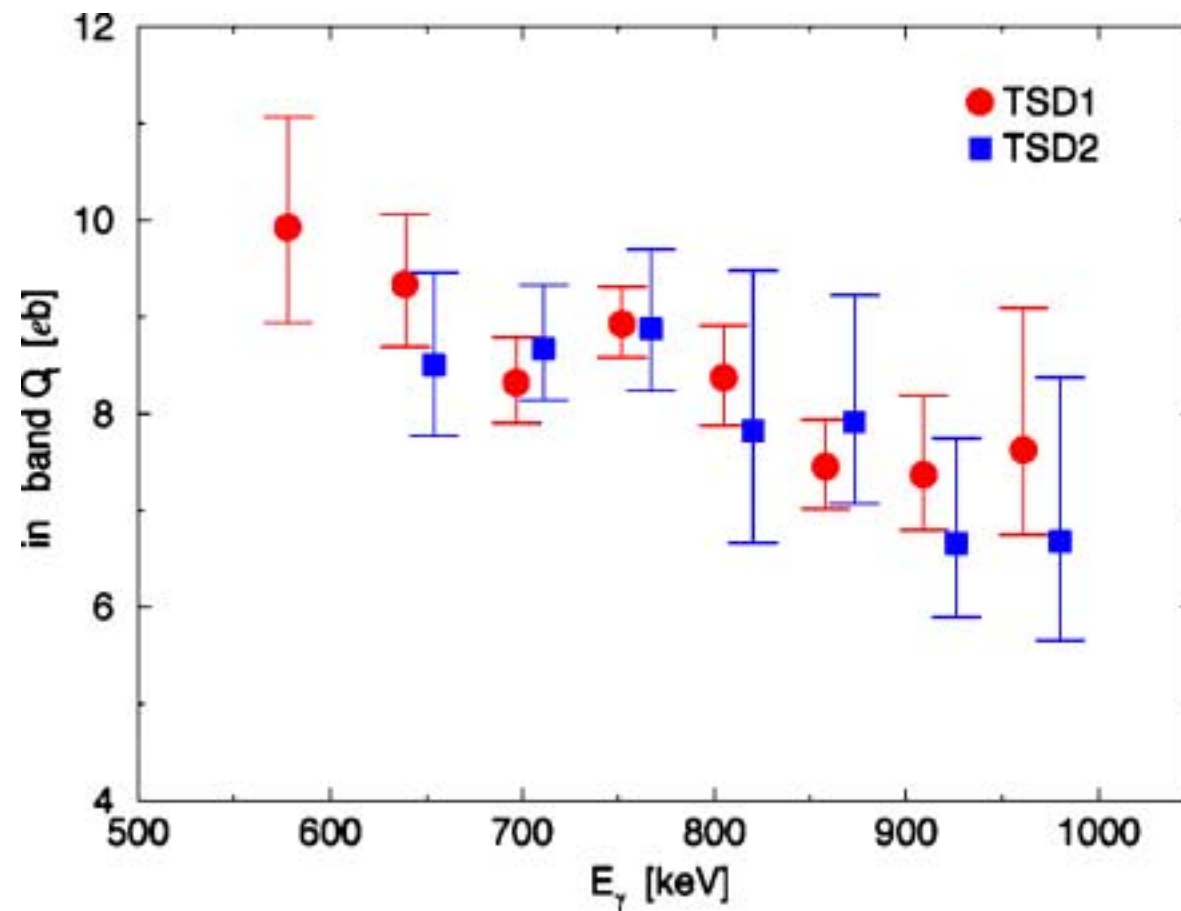
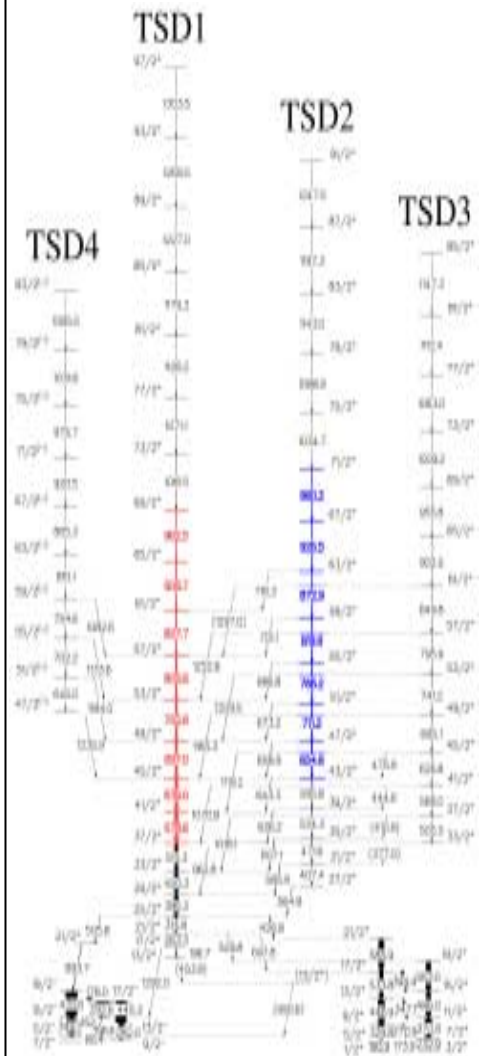


UNIVERSITY
OF OSLO

Transition quadrupole moments

A. Grgeren et al., Phys. Rev. C **69** (2004), 031301R

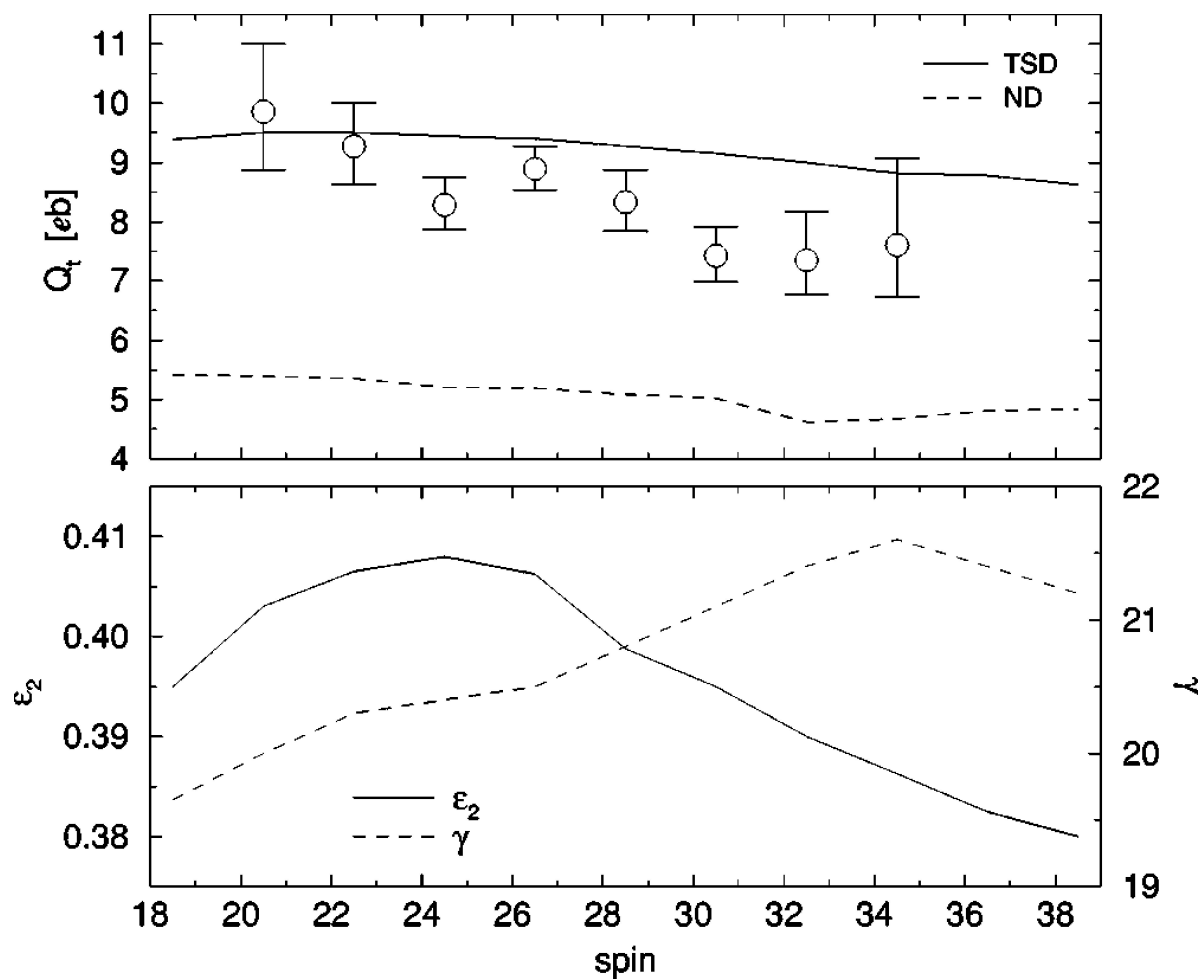
2004





UNIVERSITY
OF OSLO

Dependence on γ



A. G3rger et al., Phys. Rev. C 69 (2004), 031301R



UNIVERSITY
OF OSLO

Wobbling summary

Characteristic large $B(E2)_{\text{out}}/B(E2)_{\text{in}}$ values which approximately fulfill the phonon rule

Good agreement with PR calculations

The wobbling frequency, $\hbar\omega_w$, can be reproduced on average for $n_w=1$, but not the spin dependence.

The observed anharmonicity $\hbar\omega_w (n_w=2) < \hbar\omega_w (n_w=1)$ can not be explained by PR calculations which only includes the $\pi i_{13/2}$ subshell coupled to the triaxial rotor

Speculation: The I dependence of in-band Q_+ 's together with constant $B(E2)_{\text{out}}/B(E2)_{\text{in}}$ for $n_w=1$ to $n_w=0$ as opposed to the expected $1/I$ dependence may be caused by a moderate increase in γ over the observed spin range.



**UNIVERSITY
OF OSLO**

Neighbouring nuclei

2004



UNIVERSITY
OF OSLO

Triaxial bands in Lu/Hf nuclei

^{162}Hf	^{163}Hf	^{164}Hf	^{165}Hf	^{166}Hf	^{167}Hf	$3 (0) 10^{-3}$ ^{168}Hf L	^{169}Hf	$1 (0) 10^{-2}$ ^{170}Hf	$7 (0)$ ^{174}Hf L	$1?(1)$ ^{175}Hf
$2 (0)$ ^{161}Lu W?	$3 (0)$ ^{162}Lu	$6 (4) 10^{-1}$ ^{163}Lu W W L	$8 (2) 10^{-1}$ ^{164}Lu L	$5 (2) 10^{-2}$ ^{165}Lu W (W) L	^{166}Lu	$5 (3) 10^{-2}$ ^{167}Lu W	$1? (1) 10^{-2}$ ^{168}Lu	^{169}Lu		

$6 (4) 10^{-1}$ ^{163}Lu W W L

Number of TSD bands observed

Number of TSD bands connected to ND

Order of strength relative to yrast

Wobbling phonon excitations

Lifetimes measured



UNIVERSITY
OF OSLO

Wobbling excitations in the region

^{165}Lu : Euroball, 2002

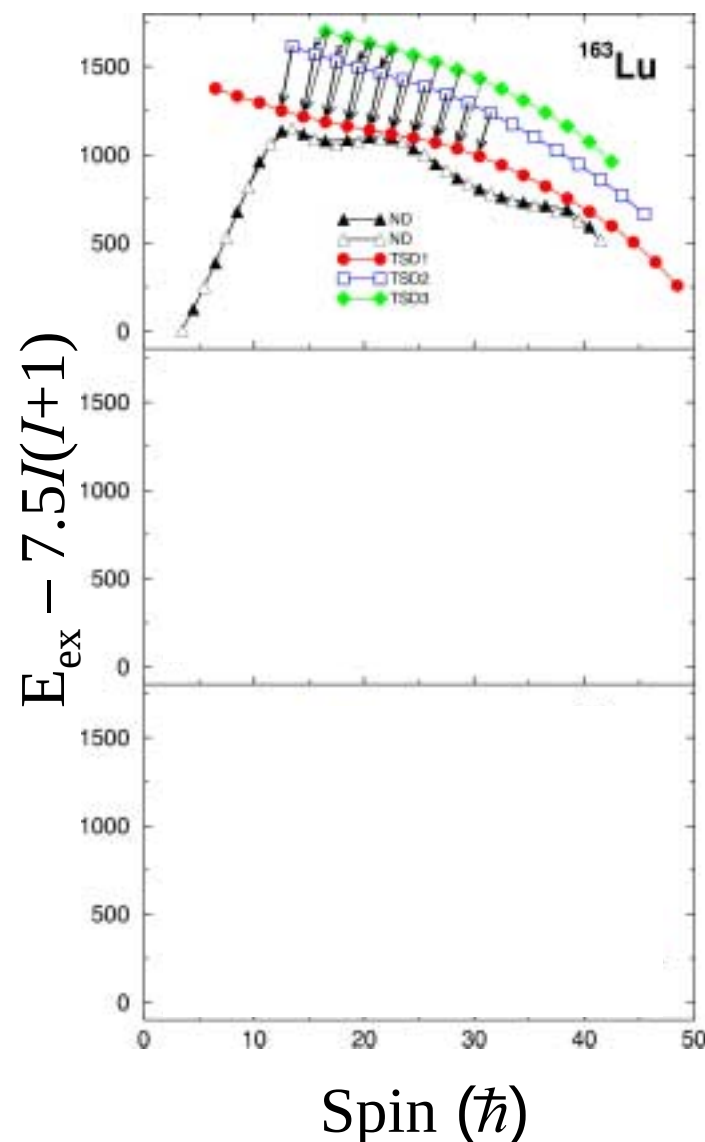
A one-phonon wobbling excitation has been firmly established, and presumably also a second-phonon band.

G. Schönwasser et al., Phys. Lett. B **552** (2003), 9.

^{167}Lu : Gammasphere, 2000

A one-phonon wobbling excitation has been firmly established.

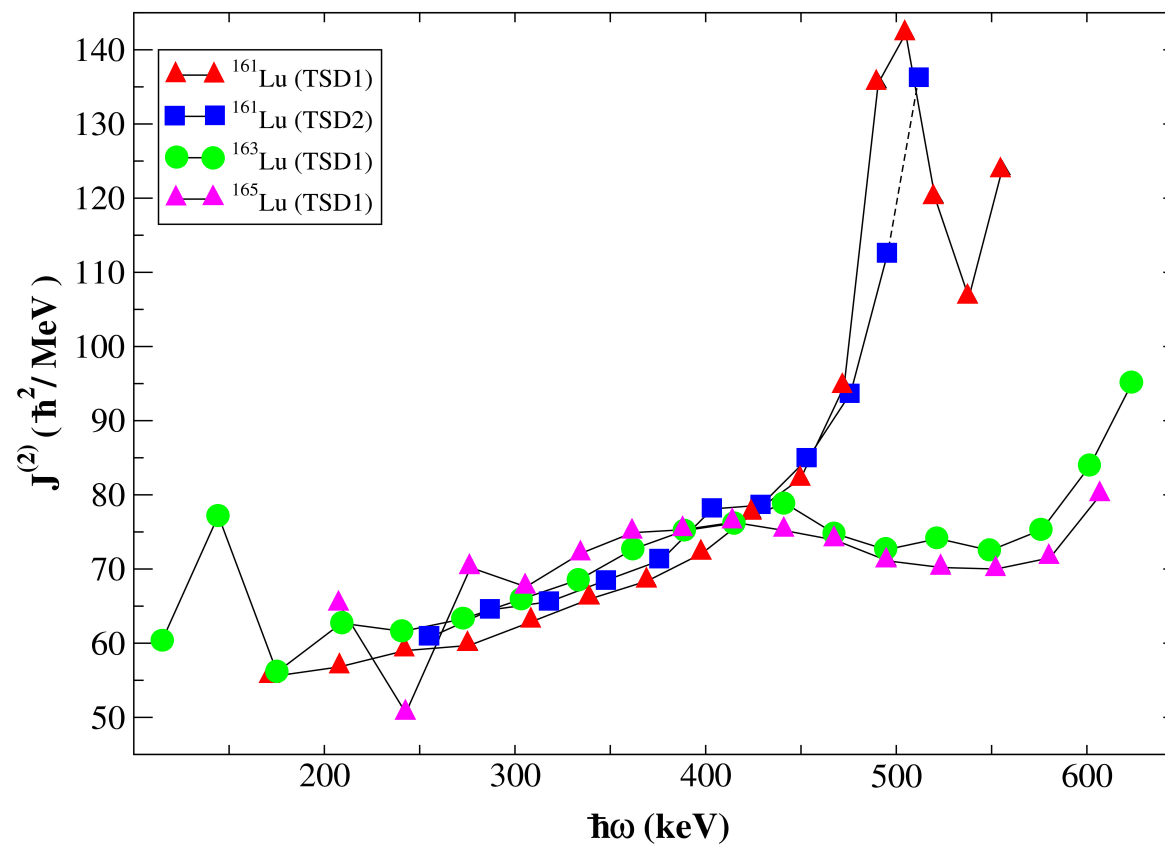
H. Amro et al., Phys. Lett. B **553** (2003), 197.





UNIVERSITY
OF OSLO

TSD in ^{161}Lu



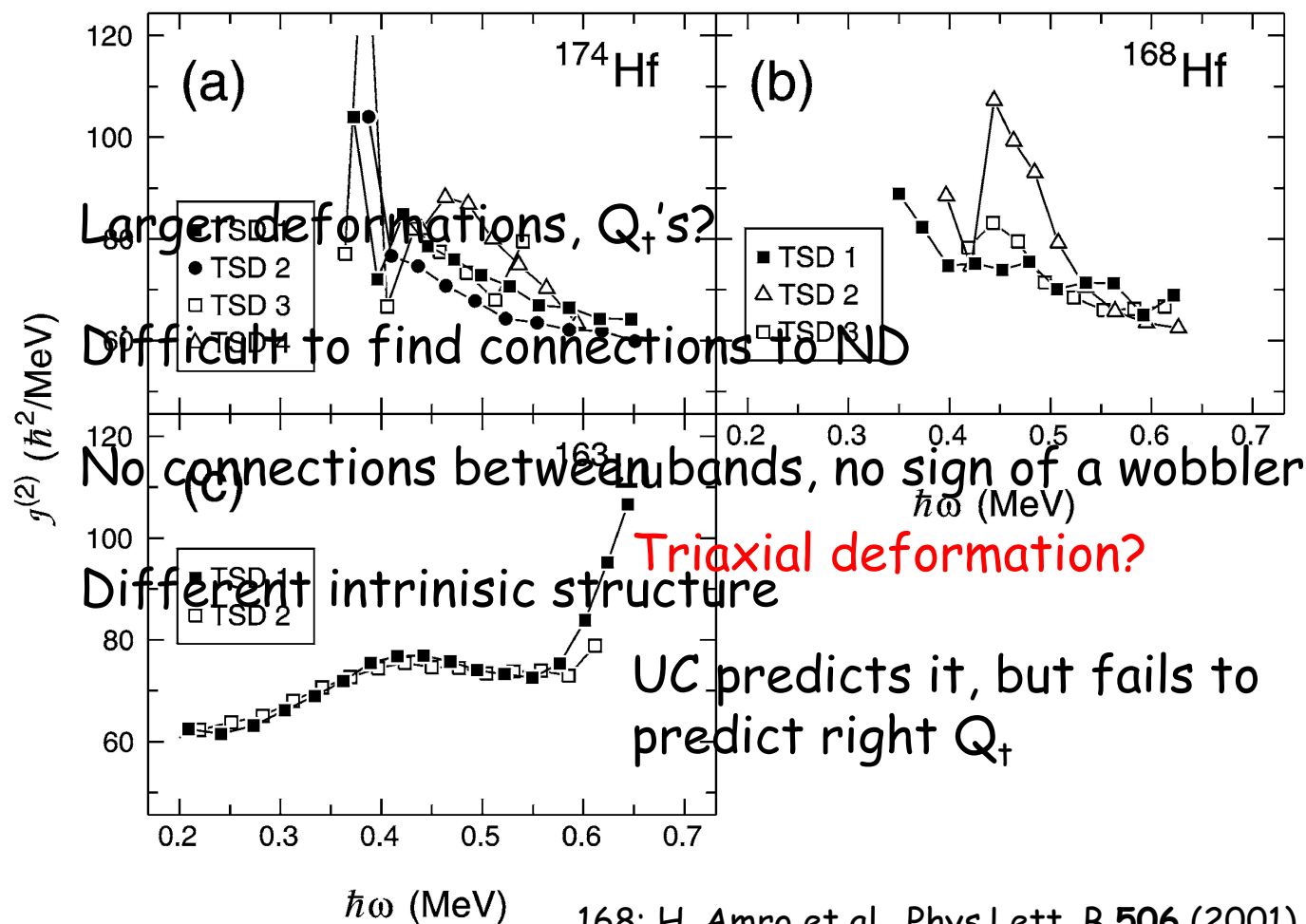
P. Bringel et al., Eur.Phys. J. A **16** (2003), 155. (GASP data)

P. Bringel et al., to be published. (EUB data)



UNIVERSITY
OF OSLO

TSD in Hafnium?



168: H. Amro et al., Phys.Lett. B **506** (2001) 39.

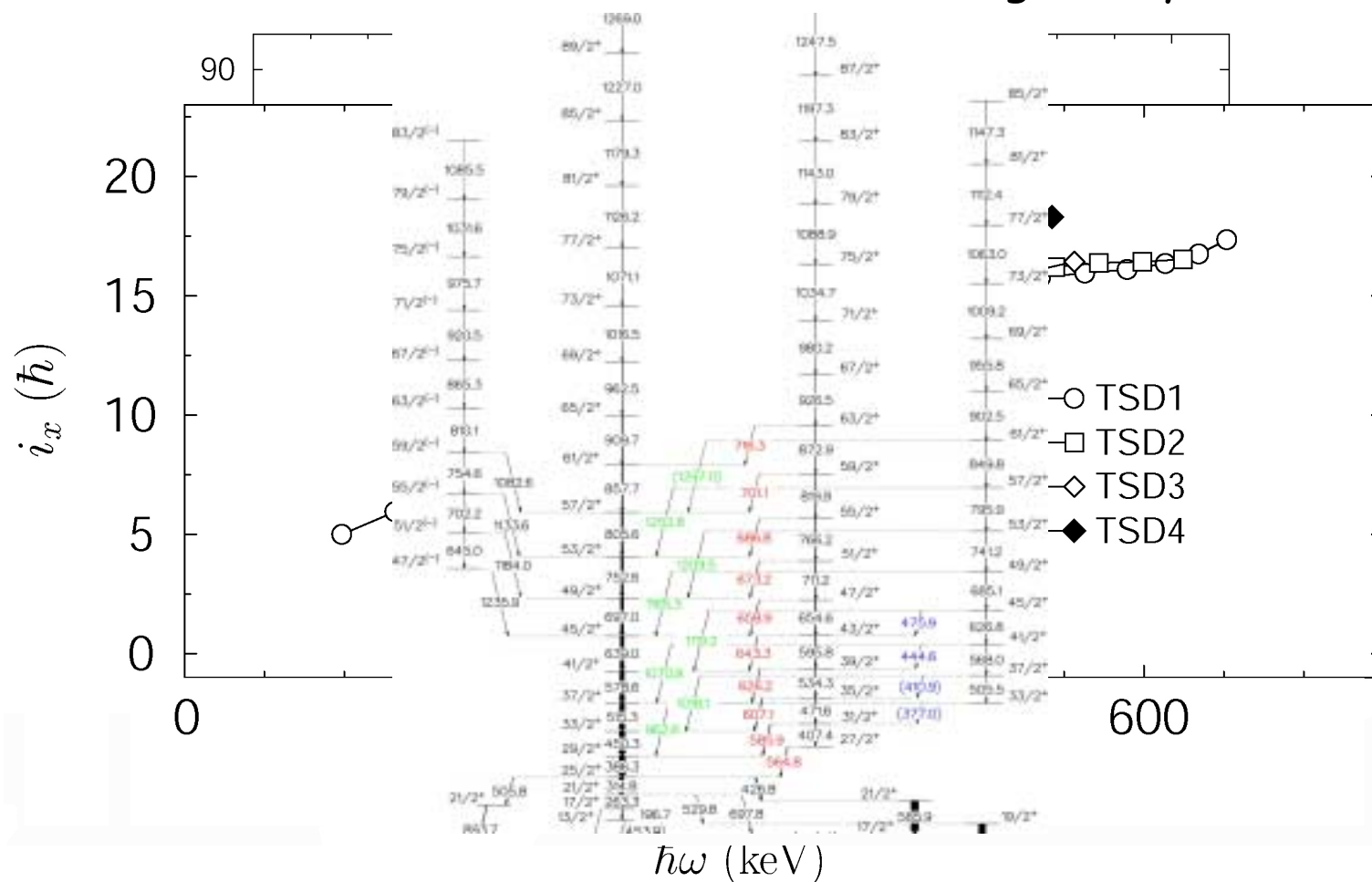
174: M. Djongolov et al., Phys.Lett. B **560** (2003) 24.



UNIVERSITY
OF OSLO

Other configurations and signature partners

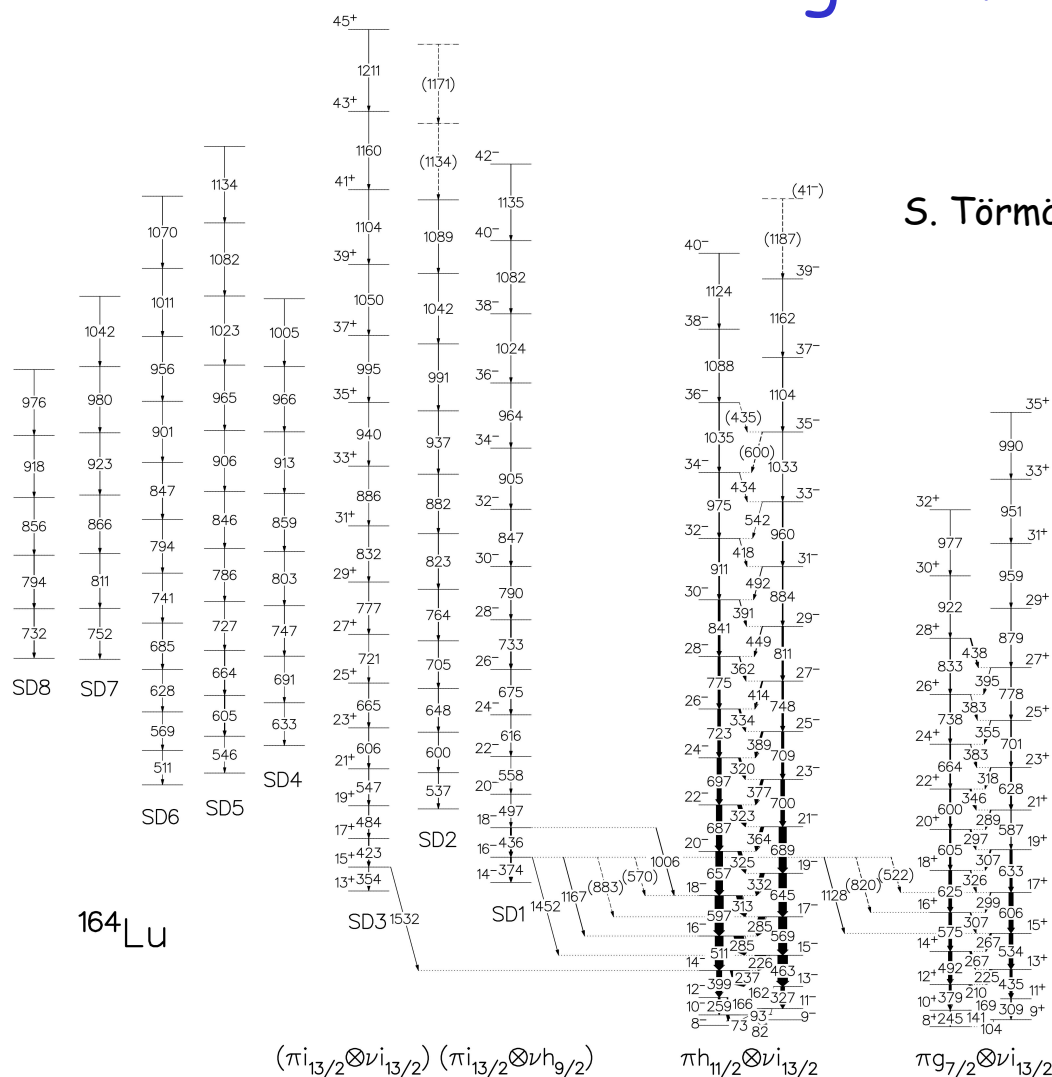
^{163}Lu : TSD 4 is not a member of the wobbling family of bands.





UNIVERSITY
OF OSLO

Other configurations and signature partners



S. Törmänen et al., Phys.Lett. B **454** (1999) 8.

^{164}Lu :

Only two of the
eight bands have
an assignment.
Possible signature
partners and
wobbling bands.

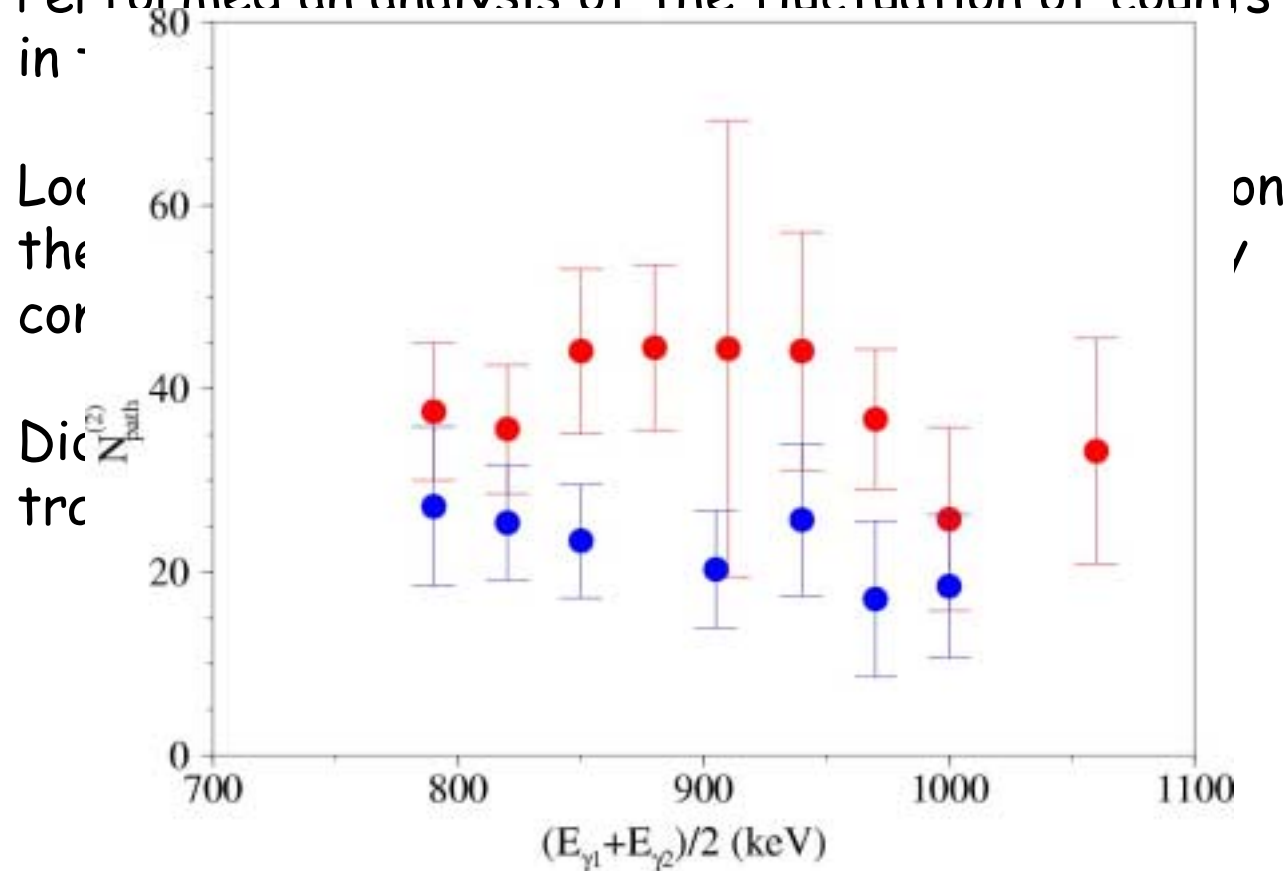
2004



UNIVERSITY
OF OSLO

Studying the quasi continuum

The number of two step paths along the TSD ridge (number of TSD bands) in ^{163}Lu gated on TSD (red) and ND (blue) transitions. Performed an analysis of the fluctuation of counts



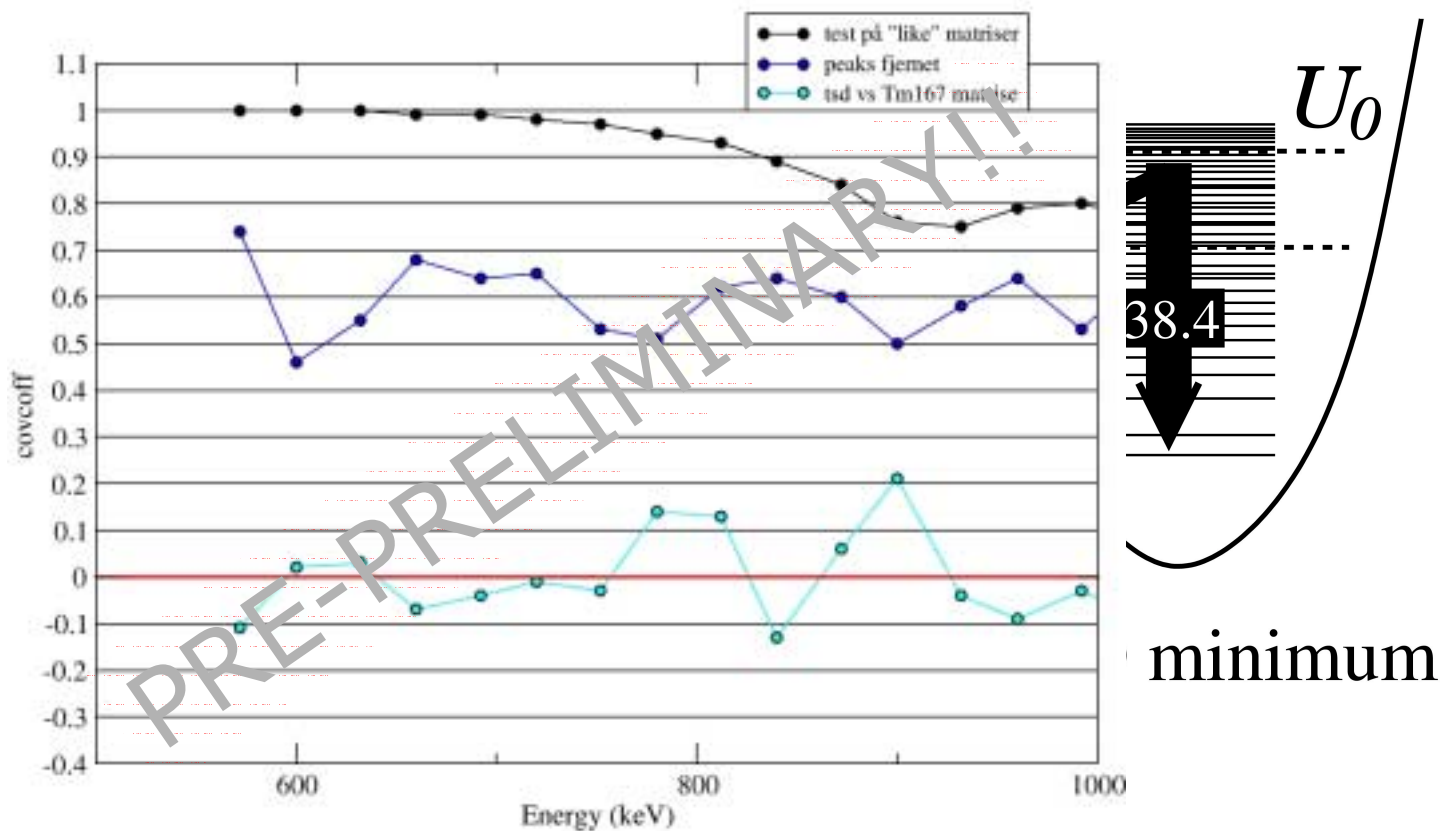
S.W. Ødegård et al., Eur. Phys. J. A **14** (2002) 309.



UNIVERSITY
OF OSLO

Studying the quasi continuum

The Covariance Analysis 40 TSD bands feed the TSD yrast
"similarity" of the two 20 TSD bands feed the ND states.





UNIVERSITY
OF OSLO

The role of *AGATA*

2004



UNIVERSITY
OF OSLO

AGATA

- . The necessary information to understand triaxiality and its effects is found in the details.
- . Need energy, precise angle and interaction points for each γ detected.
- . Need to pick out the correct γ 's of interest (which are very weak within the reaction channel)
- . Need to find and understand linking transitions
- . To explore the boundaries of this mass region and to find stable triaxiality in other mass regions.
- . AGATA does have a mission, even with stable beams



UNIVERSITY
OF OSLO

Triaxiality and Wobbling with AGATA

The bottom line

- . The Lu-Hf region is rich in strongly deformed triaxial band structures coexisting with normal deformed structures
- . The triaxiality is proven by the observation of the one- (and two-phonon wobbling excitation) in several nuclei
- . New experimental results lead to new questions. There is still a lot to learn and understand
- . Agata is a tool with the sensitivity needed to further probe and reveal the nature of triaxiality in nuclei



UNIVERSITY
OF OSLO

Collaborating institutions

NBI, Univ. of Copenhagen
Univ. Of Oslo
Univ. of Lund
Univ. of Bonn
Univ. of Milano
Univ. of Padova
INFN, Legnaro
Univ. of Camerino
Inst. of Nucl. Phys, Krakow

Univ. of Liverpool
Univ. of Paisley
Argonne Natl. Lab
Mississippi State Univ.
Univ. of Tennessee
LBL Berkeley
IReS Strasbourg
Yale Univ.