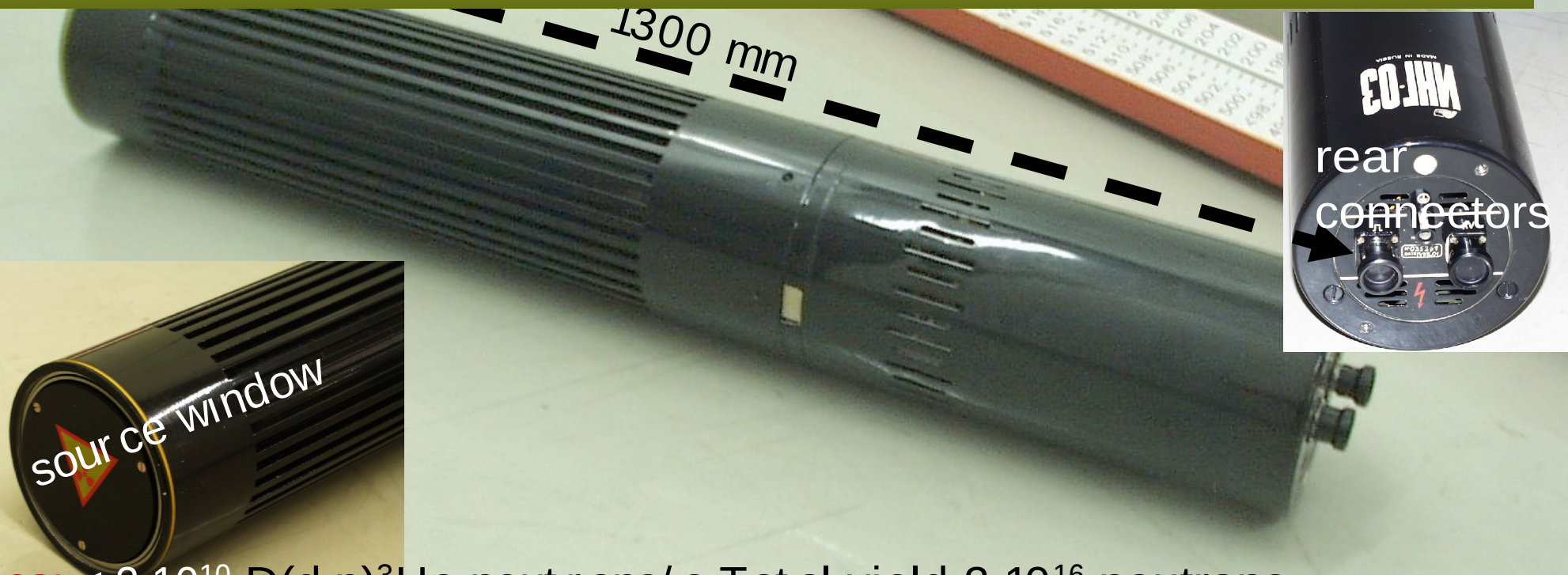




Interactions of Neutrons *with Matter*

Commercial Neutron Generator I NG- 03

Neutrons can be produced in a variety of reactions, e.g., in nuclear fission reactors or by the $D(d,n)^3\text{He}$ or $T(d,n)^4\text{He}$ reactions



Specs: $< 3 \cdot 10^{10}$ $D(d,n)^3\text{He}$ neutrons/s Total yield $2 \cdot 10^{16}$ neutrons

Pulse frequency 1-100Hz Pulse width $> 0.8 \mu\text{s}$, Power 500 W

Alternative option:
 $T(d,n)^4\text{He}$, $E_n \approx 15 \text{ MeV}$

Source: All-Russian Research Institute of
Automatics **VNIIA**

Nuclear Interactions of Neutrons

No electric charge $\rightarrow$ no direct atomic ionization $\rightarrow$ only collisions and reactions with nuclei $\rightarrow 10^{-6}$ x weaker absorption than charged particles

Processes depend on available n energy E_n :

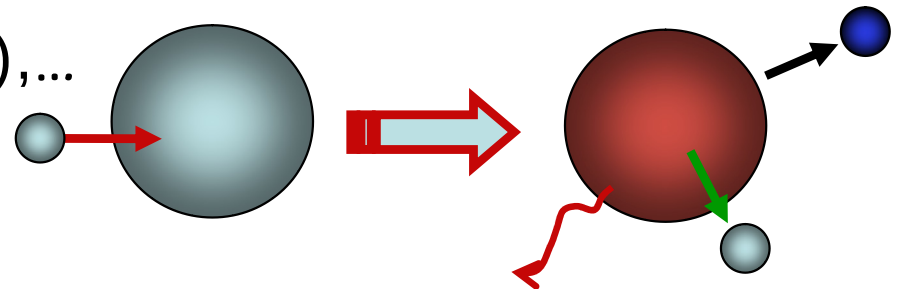
$E_n \sim 1/40$ eV ($= k_B T$) Slow diffusion, capture by nuclei

$E_n < 10$ MeV Elastic scattering, capture, nucl. excitation

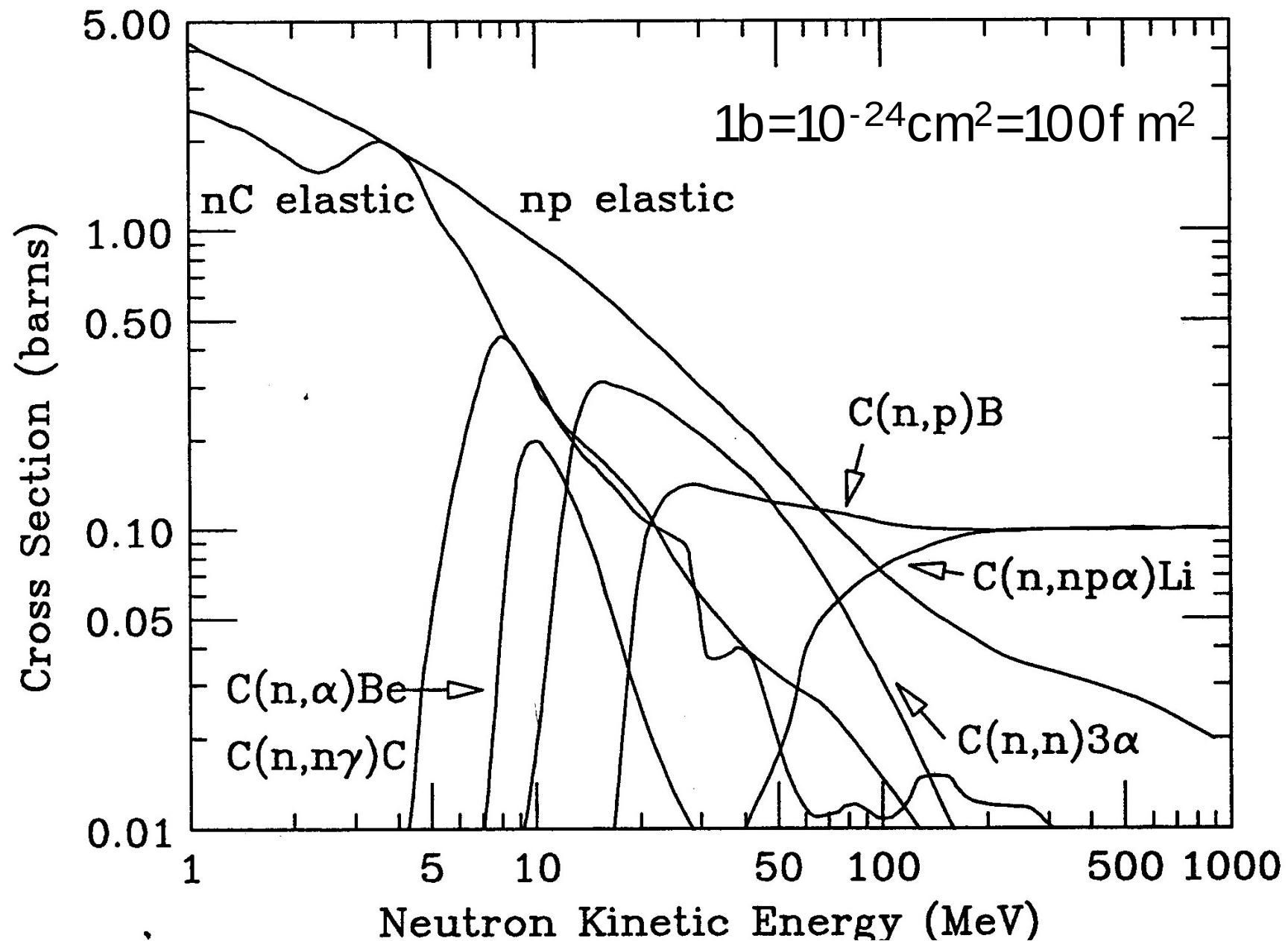
$E_n > 10$ MeV Elastic+inel. scattering, various nuclear reactions, secondary charged reaction products

Characteristic secondary nuclear radiation/ products:

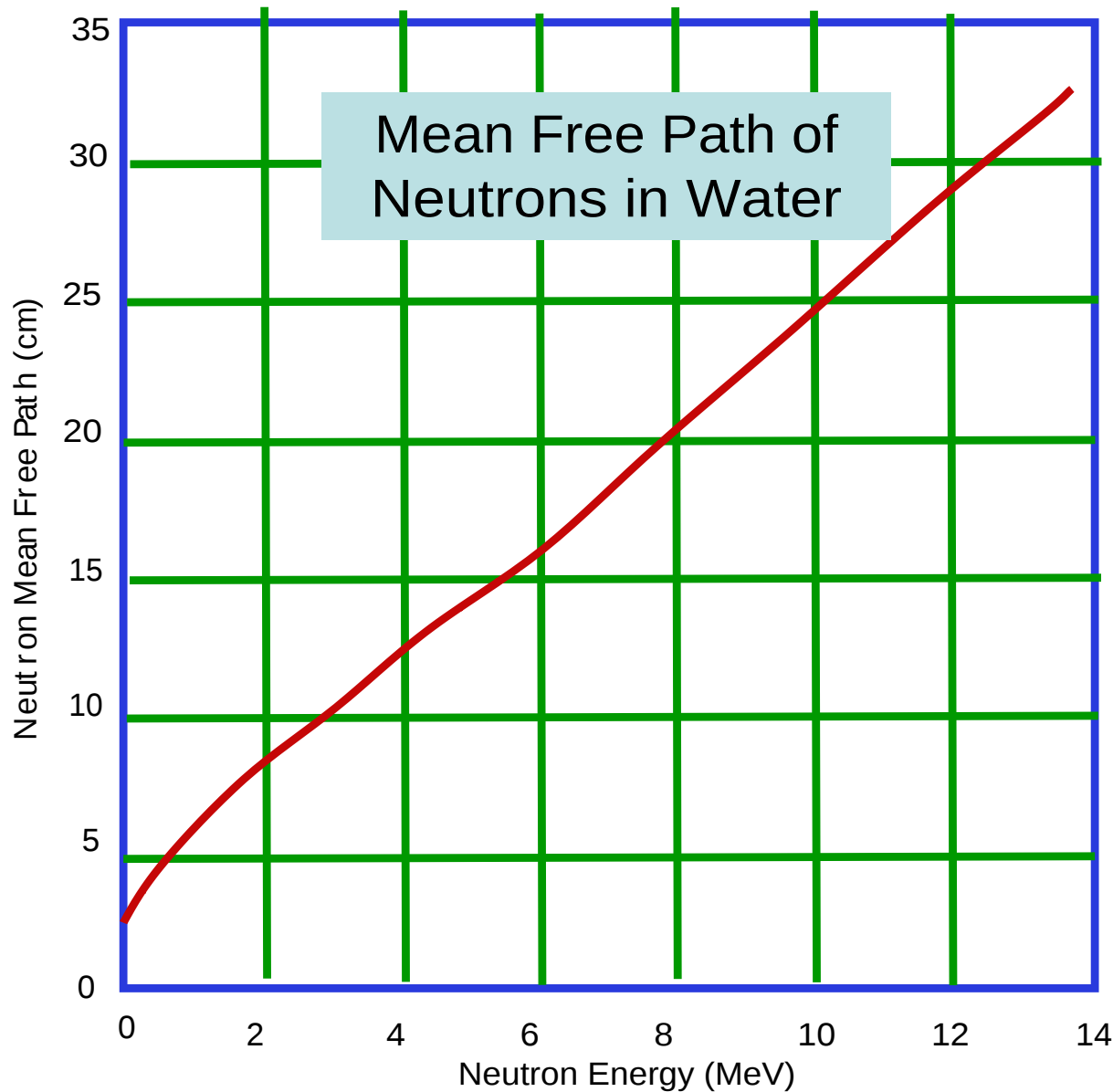
1. γ -rays (n, γ)
2. charged particles (n,p), (n, α),...
3. neutrons (n,n'), (n,2n'),...
4. fission fragments (n,f)



Neutron Cross Sections



Neutron Mean Free Path



$$N(x) = N(0)e^{-x/\lambda}$$

$$\lambda = \frac{1}{\mu} = \frac{1}{\rho\sigma} \quad mfp$$

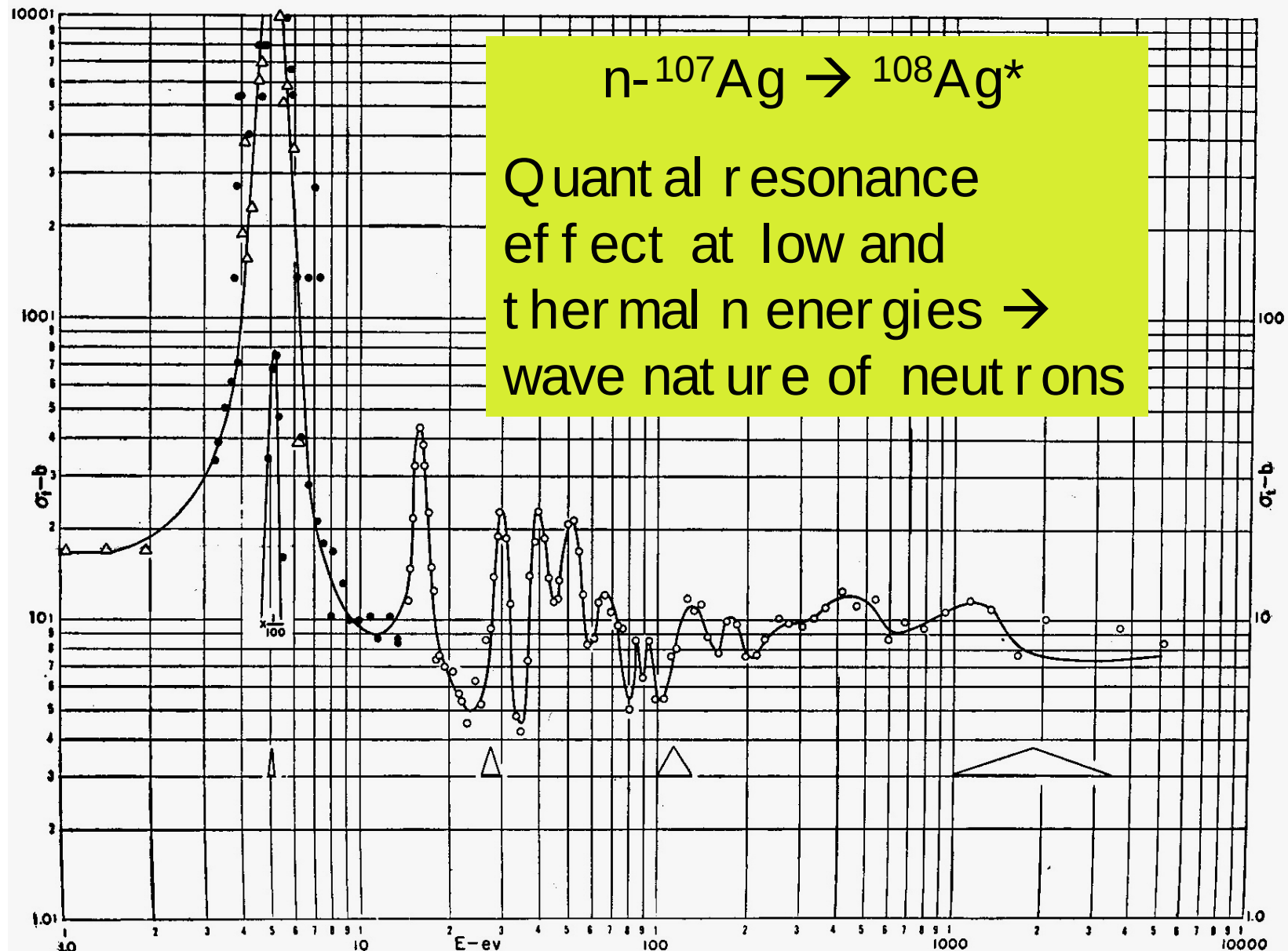
ρ : atomic density

σ : cross section

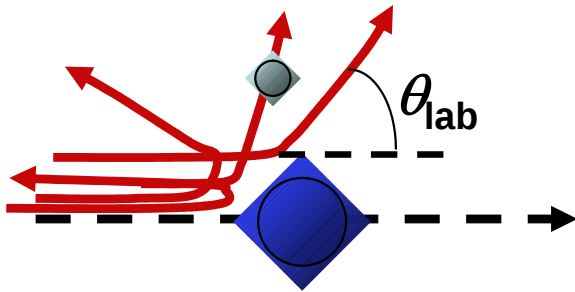
λ = average path length in medium between 2 collisions

$$\Gamma_{FWHM} = 2.35 \cdot \sigma$$

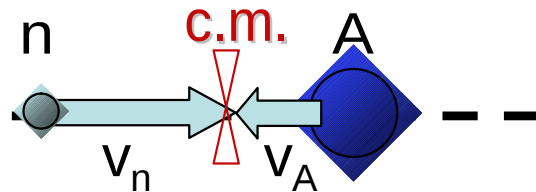
Neutron Resonance Capture



Energy Transfer in Elastic Scattering



Neutron with lab velocity v , energy E , scatters randomly off target nucleus of mass number A at rest in lab.



$$c.m.: p_n = -p_A \quad p_n + p_A = 0$$

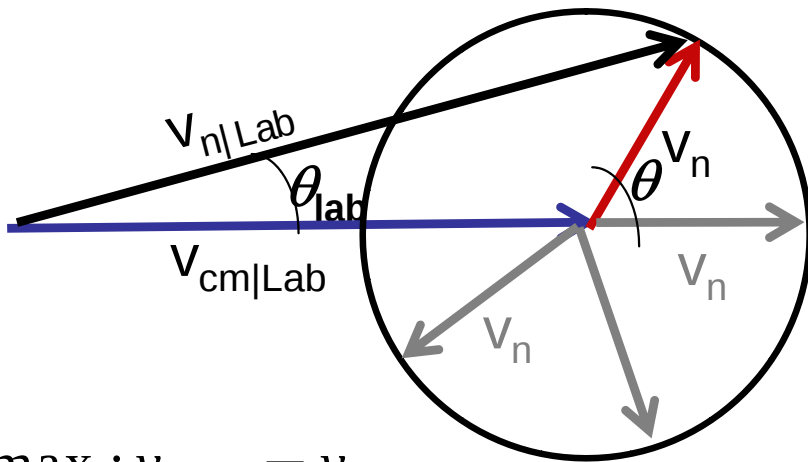
$$v_n = v \frac{A}{A+1} \quad v_A = -v \frac{1}{A+1}$$

$$v_{cm|Lab} = v \frac{1}{A+1} \quad \text{lab velocity of center of gravity}$$

$$\text{max, min: } v_{n|Lab} = v_{cm|Lab} \pm v_n$$

$$\text{max: } E_{n|Lab} = E$$

$$\text{min: } E_{n|Lab} = E \frac{(A-1)^2}{(A+1)^2}$$



$$\text{max: } v_{n|Lab} = v$$

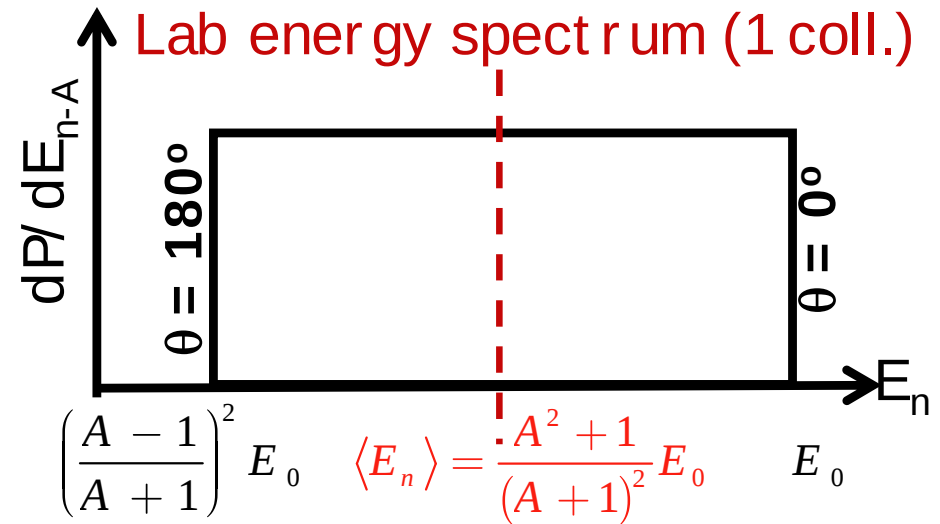
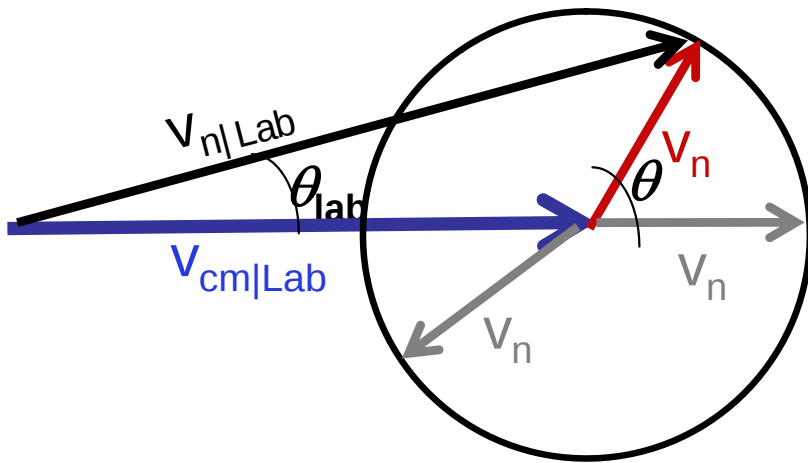


$$\text{min: } v_{n|Lab} = v \frac{A-1}{A+1}$$



Neutron Energy Spectrum

Neutron with energy E_0 scatters off target nucleus A at rest in lab.



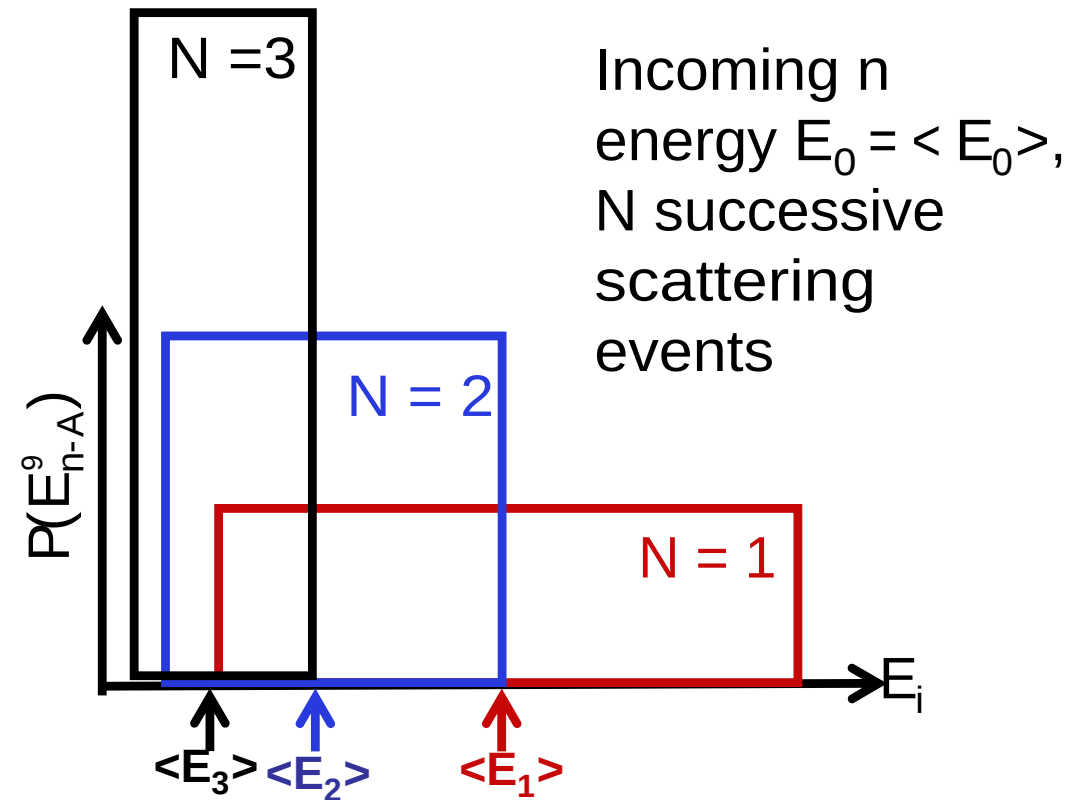
$$E_{n|Lab} \propto v_{n|Lab}^2 = \left(\vec{v} + \vec{v}_{cm|Lab} \right)^2 = \dots 2v^2 \frac{A}{(A+1)^2} \cos q$$

$$\frac{dE_{n|Lab}}{dq} \propto \sin q \rightarrow \frac{dE_{n|Lab}}{d\Omega} \propto \frac{dE_{n|Lab}}{\sin q dq} = \text{const.}$$

$$\Rightarrow \frac{ds_{n-A}(q)}{d\Omega} \propto \frac{ds_{n-A}(E_{n|Lab})}{dE_{n|Lab}} \propto \frac{dP_{n-A}(E_{n|Lab})}{dE_{n|Lab}}$$

The laboratory energy spectrum of scattered neutrons reflects the center-of-mass scattering angular distribution !

Multiple n- A Scattering



$$\langle E_1 \rangle = \left[\frac{A^2 + 1}{(A + 1)^2} \right]^1 E_0 = a^1 \langle E_0 \rangle$$

$$\langle E_2 \rangle = a \langle E_1 \rangle = a^2 \langle E_0 \rangle$$

.....

$$\langle E_N \rangle = a \langle E_{N-1} \rangle = a^N \langle E_0 \rangle$$

$$\Rightarrow P(E_1) = \frac{1}{(1 - a)E_0}$$

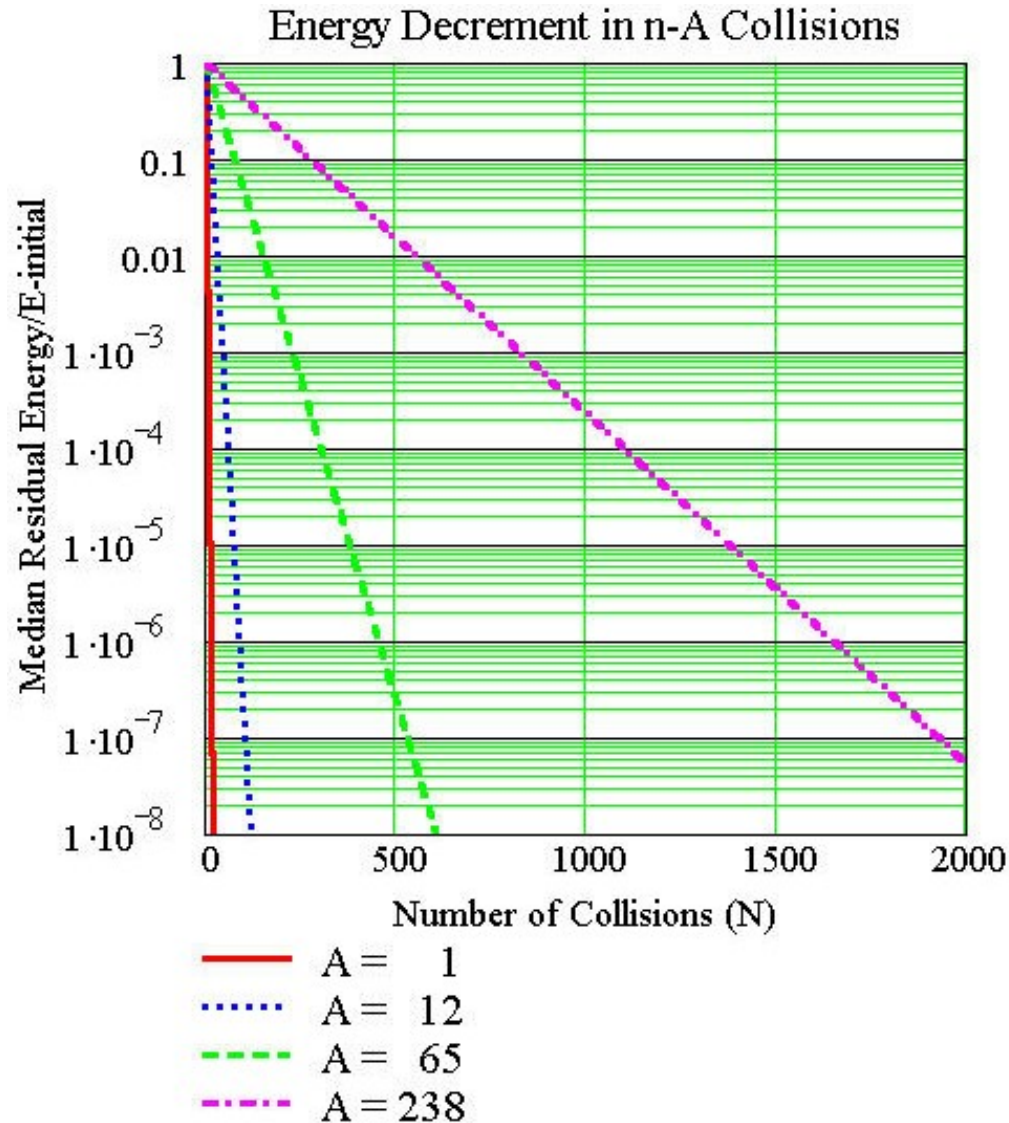
$$x := \left\langle \ln \left(E_0 / E_1 \right) \right\rangle = \int_{aE_0}^{E_0} dE \ln \left(\frac{E_0}{E} \right) P(E) = \frac{1}{(1 - a)} \int_1^a dE \ln E =$$

"Logarithmic
Decrement" ξ

$$= \frac{[x \ln x - x]_1^a}{(1 - a)} = 1 + \frac{a \ln a}{(1 - a)} = 1 + \frac{A^2 + 1}{2A} \ln \left(\frac{A^2 + 1}{(A + 1)^2} \right) \xrightarrow{A > 10} \frac{2}{A + 2/3} \neq f(E_0)$$

$$\langle \ln E_N \rangle = \langle \ln E_0 \rangle - N\xi$$

Thermalization Through Scattering



$$\langle \ln E_N \rangle = \langle \ln E_0 \rangle - n \chi$$

Define $\tilde{E}$ as median (<mean)

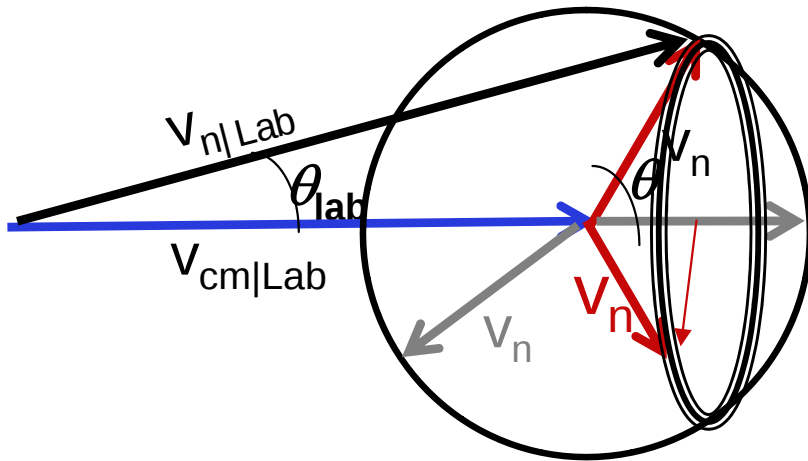
$$\ln \tilde{E} := \langle \ln E_N \rangle = \langle \ln E_0 \rangle - N \chi$$

$$\boxed{\tilde{E}(N) = E_0 \cdot e^{-N \chi}}$$

N-therm: $E_0 = 2 \text{ MeV} \rightarrow 0.025 \text{ eV}$

A	ξ	N- therm
1	1.0000	18
12	0.1578	115
65	0.0305	597
238	0.0084	2172

11



$$\begin{aligned} v_n &= \frac{v}{A+1} A & v_{cm|Lab} &= \frac{v}{A+1} \\ \vec{v}_{n|Lab}^2 &= (\vec{v}_n + \vec{v}_{cm|Lab})^2 = \\ &= \frac{v^2}{(A+1)^2} [A^2 + 1 + 2A \cos q] \end{aligned}$$

$$v_n^2 = v_{n|Lab}^2 + v_{cm|Lab}^2 - 2v_{n|Lab}v_{cm|Lab} \cos q_{Lab} \quad | : v^2 / (A + 1)^2$$

$$A^2 = \left[A^2 + 1 + 2A \cos q \right] + 1 - 2\sqrt{A^2 + 1 + 2A \cos q} \cos q_{Lab}$$

$$\cos q_{Lab} = \frac{1 + A \cos q}{\sqrt{A^2 + 1 + 2A \cos q}}$$

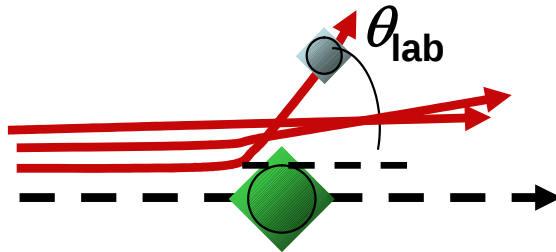
$$\langle \cos q_{Lab} \rangle = \frac{1}{2} \int_{-1}^{+1} d \cos q \frac{1 + A \cos q}{\sqrt{A^2 + 1 + 2A \cos q}} = \frac{2}{3A} \left\{ \begin{array}{l} >0 \rightarrow \\ \text{f or w a r d} \\ \text{s c a t t e r i n g} \end{array} \right.$$

A Dependence of Angular Distribution

Properties of n scattering depends on the sample mass number A

➔ Measure time-correlated flux of transmitted or reflected neutrons

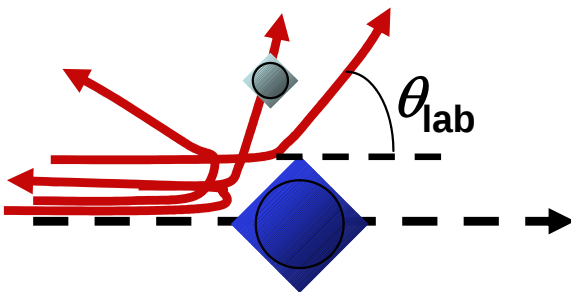
Light Nucleus



$$\langle \cos q_{lab} \rangle = 2 / (3A) \propto A^{-1} \text{ average}$$

$$\langle q_{lab} \rangle \sim \frac{p}{2} - \frac{2}{3A}$$

Heavy Nucleus



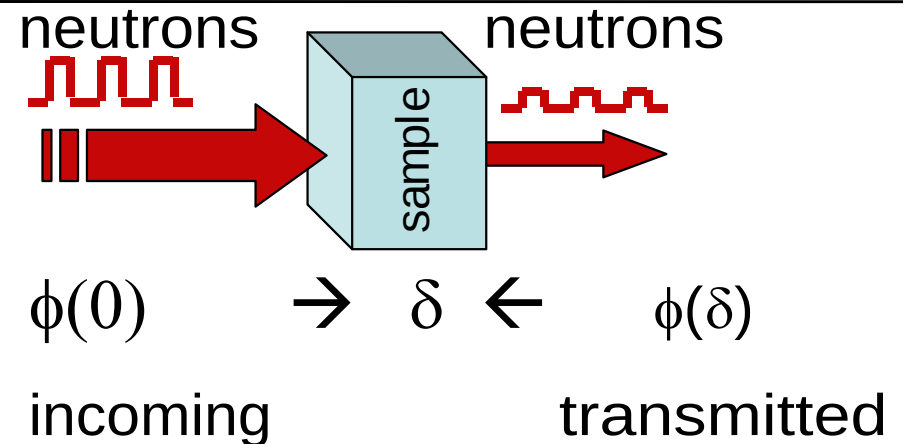
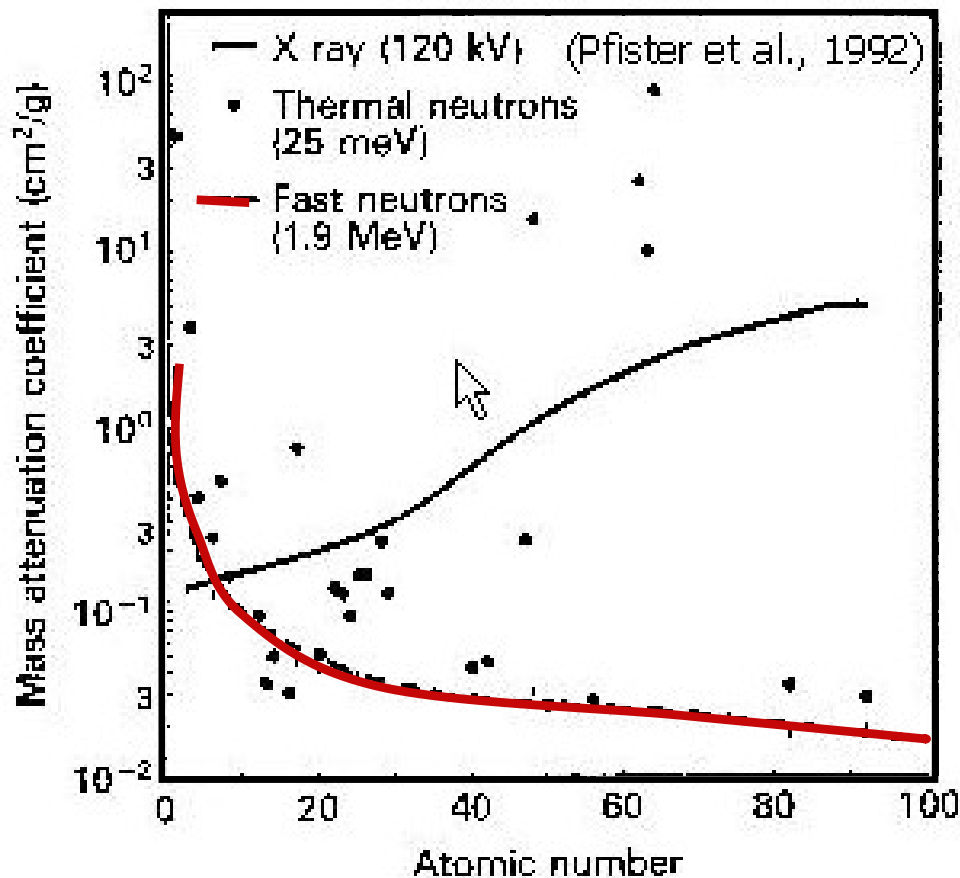
$$\tilde{E}(N) \approx E_0 \cdot \exp \left\{ \frac{-2N}{(A + 2/3)} \right\}$$

(After N collisions)

Light nuclei: slowing-down and diffusion of neutron flux

Heavy nuclei: neutrons lose less energy, high reflection/transmission

Principle of Fast-Neutron Imaging (2)



$$\phi(\delta) = \phi(0) \cdot T(\delta)$$

$$T(\delta) = e^{-\Sigma \cdot d} \text{ Transmission}$$

$$\Sigma = \mu \cdot \rho = N_A \cdot \sigma_A \cdot \rho$$

$$\mu = \text{atten. coeff}$$

$$\rho = \text{material density}$$

Transmission decreases exponentially (reflectivity increases) with thickness and density of sample, for most materials.

Neutron Diffusion

Multiple scattering = statistical process

Heavy materials ($A \gg 1$): random scattering

$$N = \frac{1}{x} \ln \left(\frac{E_0}{E_1} \right) \quad \text{Number of collisions } E_0 \rightarrow E_1$$

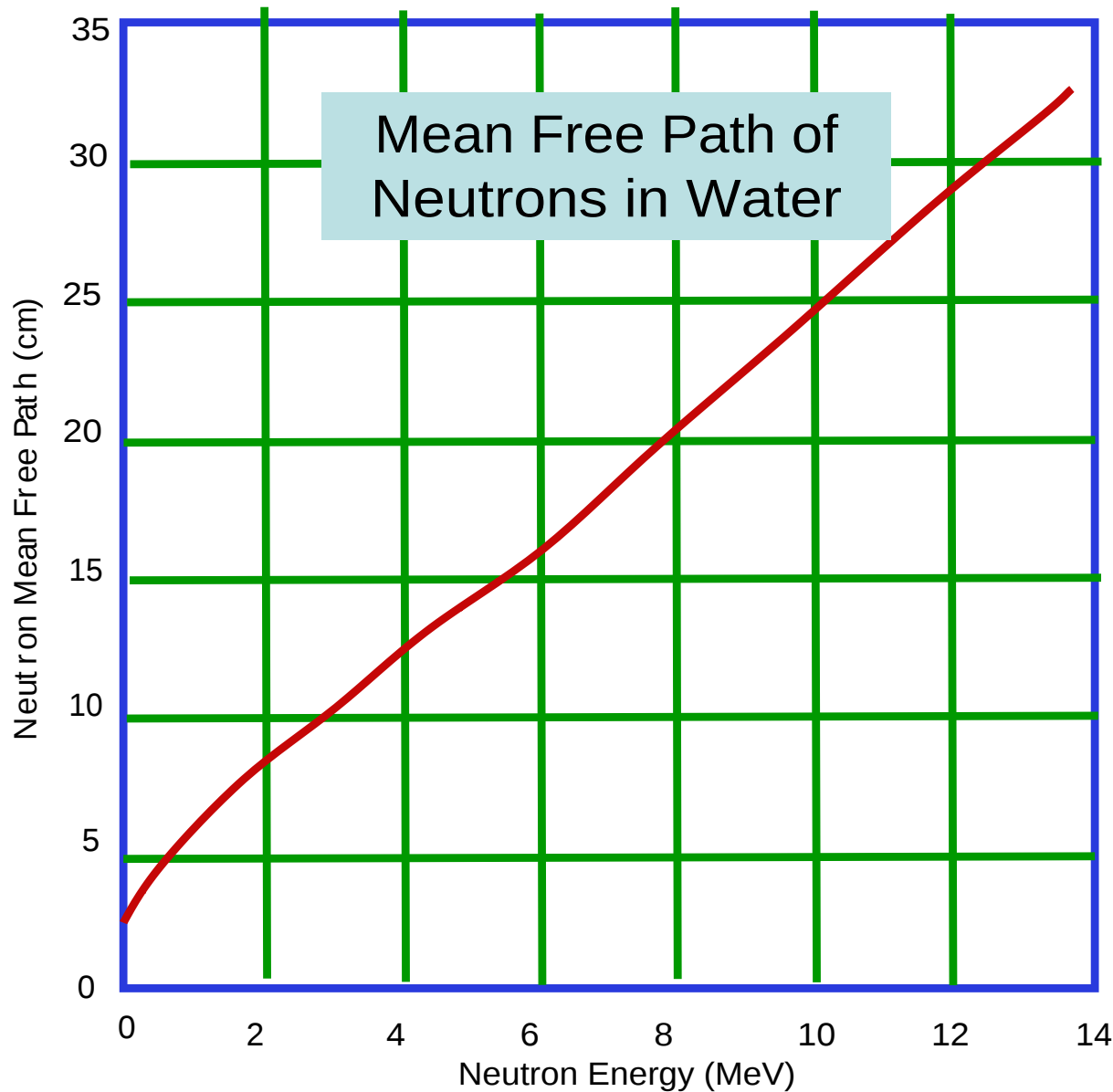
Probability for no collision along path length x : $P(x)$

$$P(x) = \frac{1}{\lambda} \cdot e^{-\frac{x}{\lambda}} \quad \text{for } \lambda = \text{const.}$$

Mean – square displacement

$$\langle x^2 \rangle_N = N \langle \lambda^2 \rangle = \int_0^\infty dx x^2 e^{-x/\lambda} / \int_0^\infty dx e^{-x/\lambda} = 2\lambda^2$$

Neutron Mean Free Path



$$N(x) = N(0)e^{-x/\lambda}$$

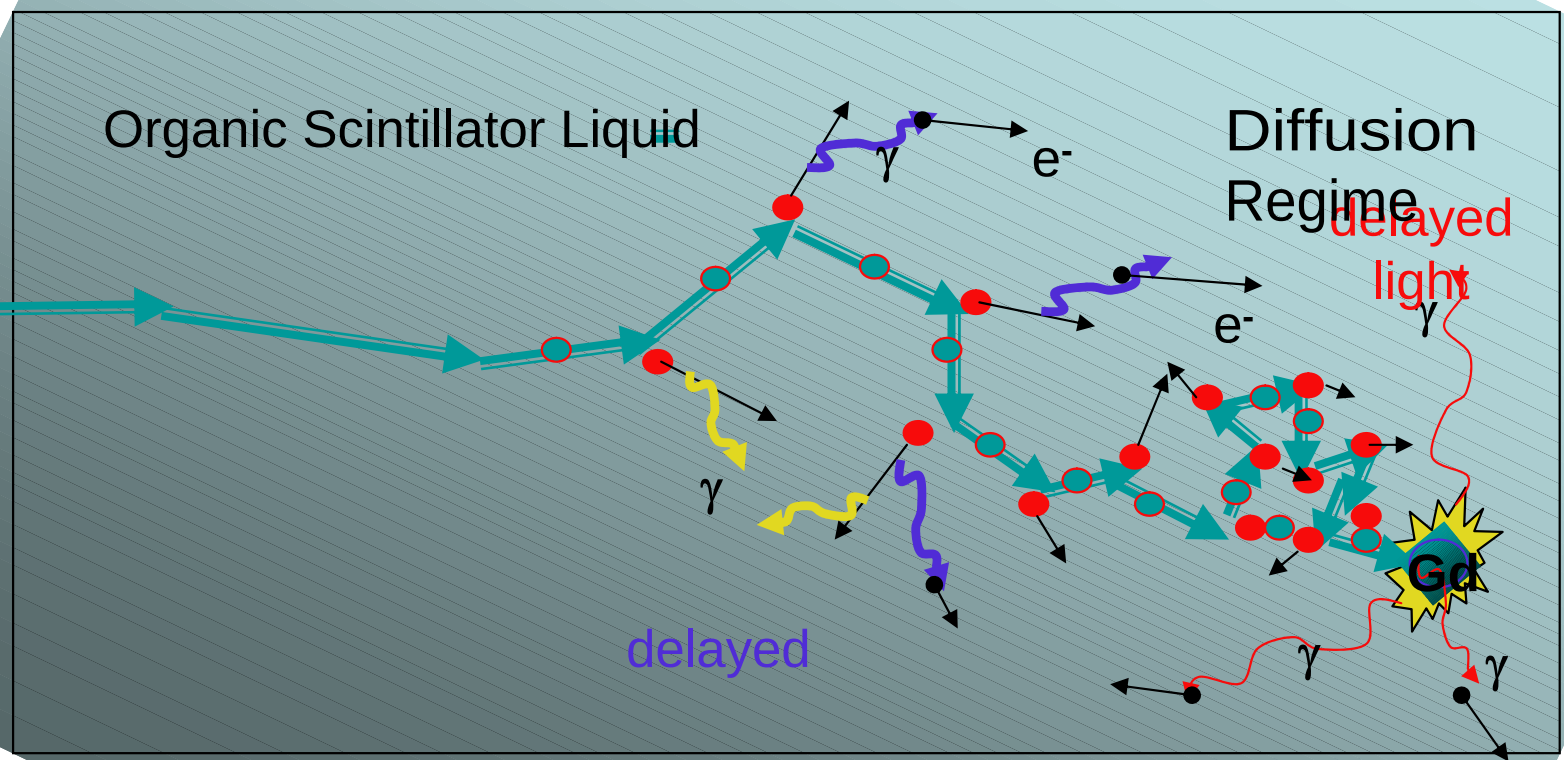
$$\lambda = \frac{1}{\mu} = \frac{1}{\rho\sigma} \quad mfp$$

ρ : atomic density

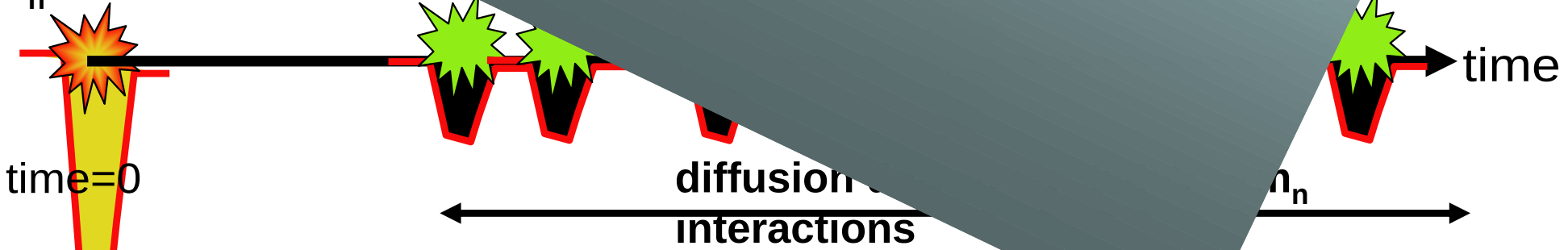
σ : cross section

λ = average path length in medium between 2 collisions

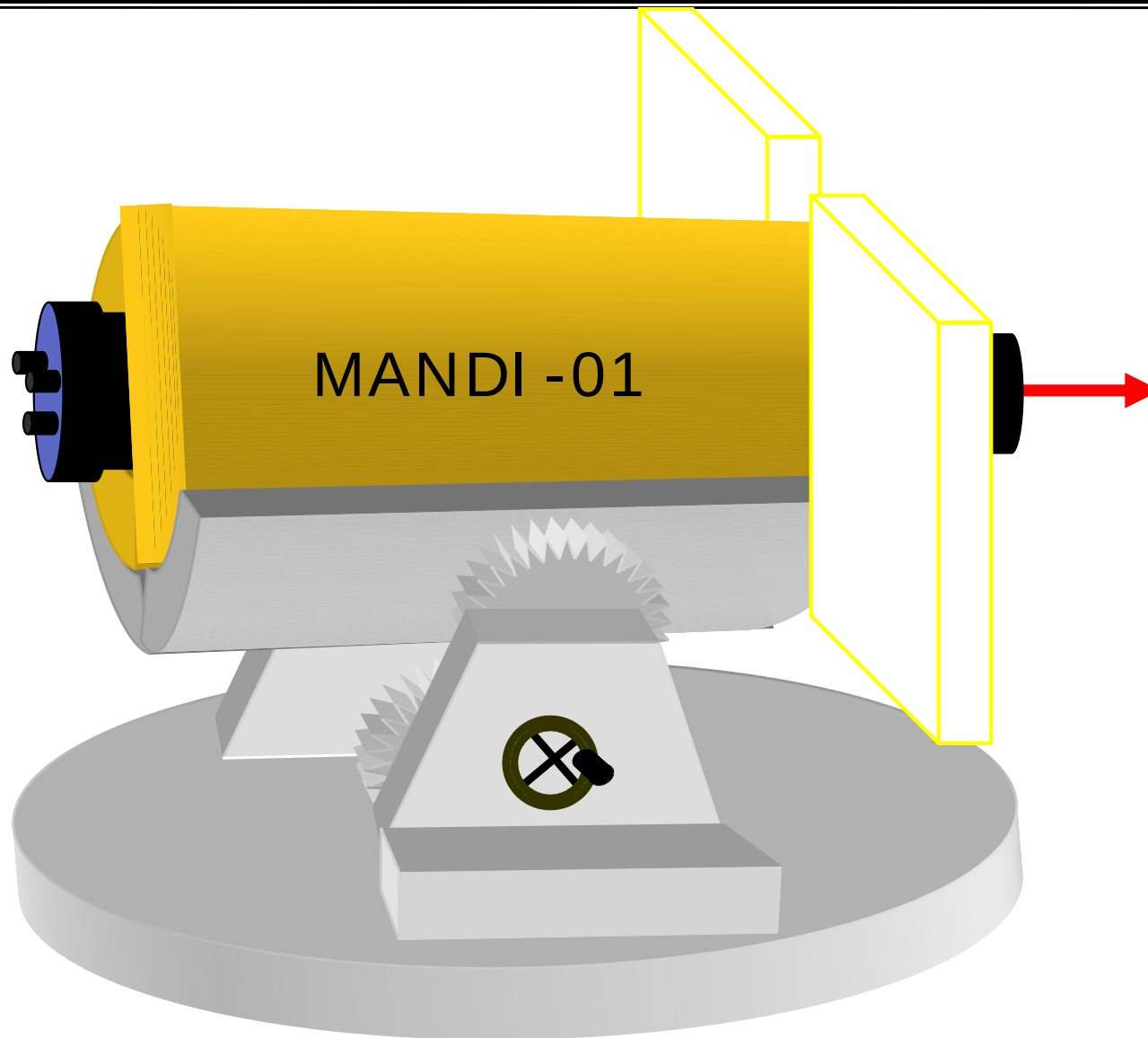
$$\Gamma_{FWHM} = 2.35 \cdot \sigma$$



Prompt
Injection of
 m_n neutrons



A Mobile Accelerator-Based Neutron Diagnostic Imager



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