

# Unraveling the dependence of the Electric Dipole Polarizability on the isovector properties of the nuclear effective interaction

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**September 19, 2013**

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# INTRODUCTION

# The Nuclear Many-Body Problem:

- ▶ **Nucleus:** from few to more than 200 strongly interacting and **self-bound fermions**.
- ▶ **Underlying interaction** is **not perturbative** at the (low)energies of interest for the study of masses, radii, deformation, giant resonances,...
- ▶ **Complex systems:** **spin, isospin, pairing, deformation, ...**
- ▶ **Many-body** calculations based on **NN scattering data** in the vacuum are feasible for the **EoS, light and light-medium nuclei**, no extensive calculations for nuclei along the whole periodic table.
- ▶ Based on effective interactions, **Nuclear Energy Density Functionals** can be successfully applied to the whole periodic table (except light systems) for the description of **masses, nuclear sizes, deformations, Giant Resonances,...**

## ...in the near future:

- ▶ **New Radioactive Beam Facilities** will measure nuclear properties far from stability: **new tests for “ab-initio” and EDF calculations**
- ▶ **The experimental study of nuclei at the meeting point ( $A \sim 40$ ) between “ab-initio” and EDFs** is now becoming and will become in the near future one of our tools ...
  - ▶ ... to **build new EDFs with improved performance** (mainly in interaction channels that are not disentangled by the usual fitting procedures with stable experimental data not from future experiments)
  - ▶ ... to **guide “ab-initio” calculations** in the description of **heavy nuclei** well described within the density functional theory.

# Approximate realization of an exact Nuclear Energy Density Functional:

## Kohn-Sham iterative scheme (static approximation)

- ▶ Determine a good  $E[\rho]$
- ▶ Initial guess  $\rho_0$
- ▶ Calculate potential  $V_{\text{eff}}$  from  $\rho_0$
- ▶ Solve single particle (Schrödinger) equation and find single particle wave functions  $\phi_i$
- ▶ Use  $\phi_i$  for calculating new  $\rho_1 = \sum_i^A |\phi_i|^2$
- ▶ Repeat until convergence

**Runge-Gross Theorem:** dynamic generalization of the static EDFs.

$$\int dt \{ \langle \Phi(t) | i\partial_t | \Phi(t) \rangle - E[\rho(t), t] \} = 0$$

Giant Resonances well described within the small amplitude limit (known as RPA approach)

# Nuclear Energy Density Functionals:

Main types of successful EDFs for the description of masses, deformations, nuclear distributions, Giant Resonances, ...

**Relativistic mean-field models**, based on Lagrangians where effective mesons carry the interaction:

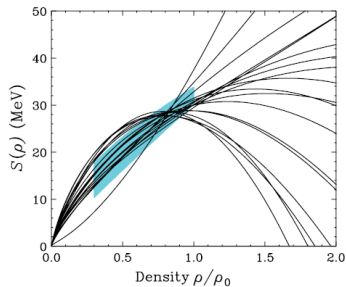
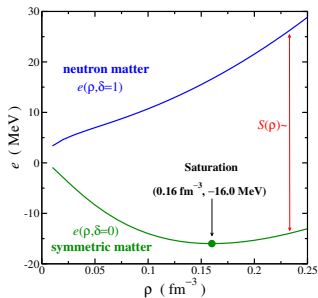
$$\begin{aligned}\mathcal{L}_{\text{int}} &= \bar{\Psi}\Gamma_{\sigma}(\bar{\Psi}, \Psi)\Psi\Phi_{\sigma} & + \bar{\Psi}\Gamma_{\delta}(\bar{\Psi}, \Psi)\boldsymbol{\tau}\Psi\Phi_{\delta} \\ &- \bar{\Psi}\Gamma_{\omega}(\bar{\Psi}, \Psi)\gamma_{\mu}\Psi\Lambda^{(\omega)\mu} & - \bar{\Psi}\Gamma_{\rho}(\bar{\Psi}, \Psi)\gamma_{\mu}\boldsymbol{\tau}\Psi\Lambda^{(\rho)\mu} \\ &- e\bar{\Psi}\hat{Q}\gamma_{\mu}\Psi\Lambda^{(\gamma)\mu}\end{aligned}$$

**Non-relativistic mean-field models**, based on Hamiltonians where effective interactions are proposed and tested:

$$V_{\text{Nucl}}^{\text{eff}} = V_{\text{attractive}}^{\text{long-range}} + V_{\text{repulsive}}^{\text{short-range}} + V_{\text{SO}} + V_{\text{pair}}$$

- ▶ Fitted **parameters contain** (important) **correlations beyond the mean-field**
- ▶ Nuclear energy functionals are **phenomenological** → **not directly connected to any NN (or NNN) interaction** (opposite to “ab-initio” calculations)

# The Nuclear Equation of State: Infinite System



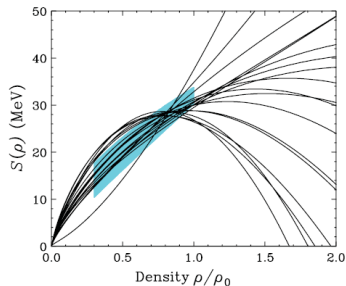
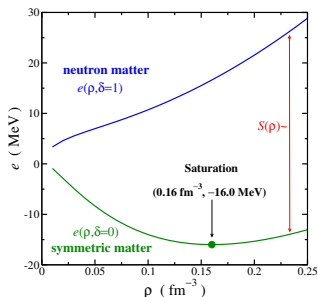
$$\frac{E}{A}(\rho, \beta) = \frac{E}{A}(\rho, \beta = 0) + S(\rho)\beta^2 + \mathcal{O}(\beta^4)$$

► Nuclear Matter

$$\left[ \beta = \frac{\rho_n - \rho_p}{\rho} \right]$$



# The Nuclear Equation of State: Infinite System



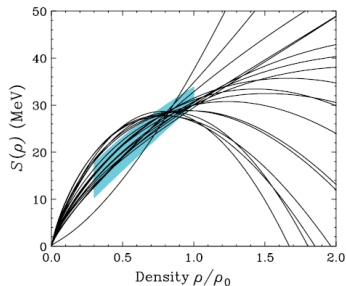
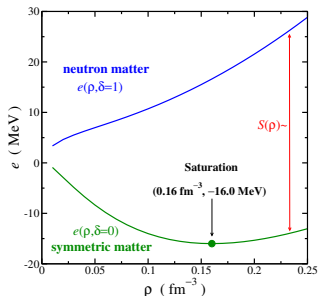
$$\frac{E}{A}(\rho, \beta) = \frac{E}{A}(\rho, \beta = 0) + S(\rho)\beta^2 + \mathcal{O}(\beta^4)$$

► Nuclear  
Matter

► Symmetric  
Matter

$$\left[ \beta = \frac{\rho_n - \rho_p}{\rho} \right]$$

# The Nuclear Equation of State: Infinite System



$$\frac{E}{A}(\rho, \beta) = \frac{E}{A}(\rho, \beta = 0) + S(\rho)\beta^2 + \mathcal{O}(\beta^4)$$

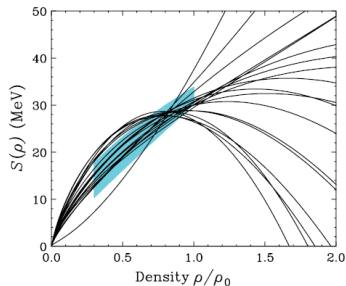
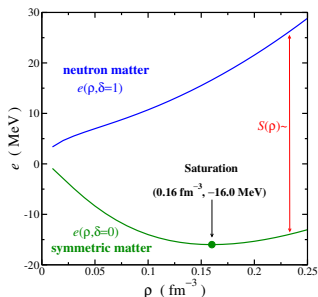
► Nuclear Matter

► Symmetric Matter

► Symmetry energy

$$\left[ \beta = \frac{\rho_n - \rho_p}{\rho} \right]$$

# The Nuclear Equation of State: Infinite System

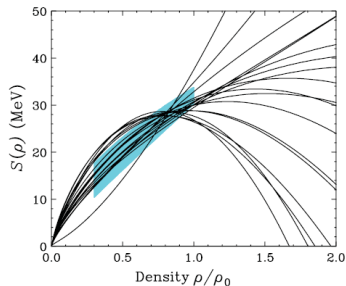
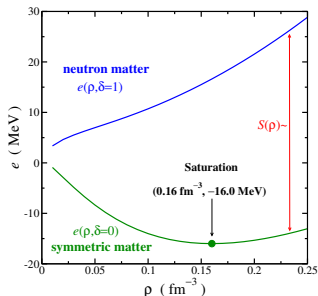


$$\frac{E}{A}(\rho, \beta) = \frac{E}{A}(\rho, \beta = 0) + S(\rho)\beta^2 + \mathcal{O}(\beta^4)$$

$$= \frac{E}{A}(\rho, \beta = 0) + \beta^2 \left( J + Lx + \frac{1}{2}K_{\text{sym}}x^2 + \mathcal{O}(x^3) \right)$$

$$\left[ \beta = \frac{\rho_n - \rho_p}{\rho}; \quad x = \frac{\rho - \rho_0}{3\rho_0} \right]$$

# The Nuclear Equation of State: Infinite System



$$\frac{E}{A}(\rho, \beta) = \frac{E}{A}(\rho, \beta = 0) + \beta^2 \left( \boxed{J} + \boxed{L} x + \frac{1}{2} \boxed{K_{\text{sym}}} x^2 + \mathcal{O}(x^3) \right)$$

►  $S(\rho_0) = J$

►  $\left. \frac{d}{d\rho} S(\rho) \right|_{\rho_0} = \frac{L}{3\rho_0} = \frac{P_0}{\rho_0^2}$

►  $\left. \frac{d^2}{d\rho^2} S(\rho) \right|_{\rho_0} = \frac{K_{\text{sym}}}{9\rho_0^2}$

$$\left[ \beta = \frac{\rho_n - \rho_p}{\rho}; \quad x = \frac{\rho - \rho_0}{3\rho_0} \right]$$

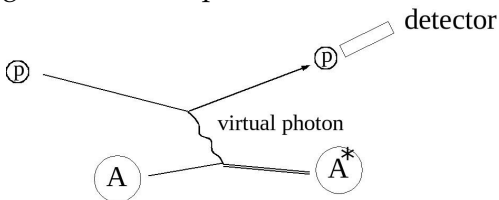
# **DIPOLE POLARIZABILITY**

# Recent measurement in $^{208}\text{Pb}$ at RCNP

At the Research Center for Nuclear Physics (RCNP), Osaka ...

- ▶ using **polarized protons**
- ▶ measuring protons **scattered inelastically**
- ▶ excitations via virtual photons (**Coulomb excitation**)
- ▶ able to cover a **broad range of excitation energies**
- ▶ set up with **high-resolution and efficiency**

Very good agreement with previous measurements is found



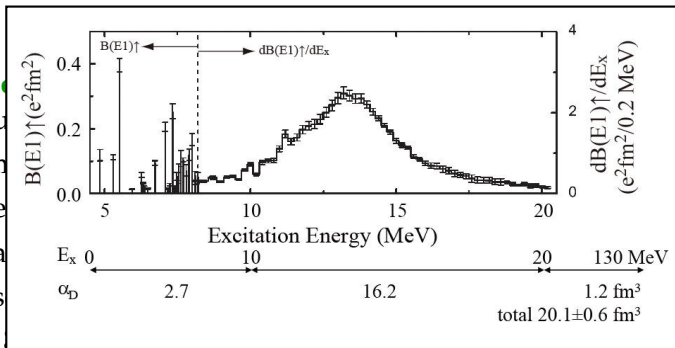
A. Tamii et al., PRL107 (2011) 062502

# Recent measurement in $^{208}\text{Pb}$ at RCNP

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and

Figure taken from A. Tamii's talk at INPC 2013

Dipole polarizability is determined with high accuracy by taking the average of the RCNP data plus available data in  $^{208}\text{Pb}^\dagger$  covering a wide range of excitation energies:  $\alpha_D = 20.1 \pm 0.6 \text{ fm}^3$

A. Tamii et al. †K. Schelhaas et al., Nucl. Phys. A 489, 189 (1988); A. Veyssiere, H. Beil, R. Bergere, P.

Carlos, and A. Lepretre, Nuclear Physics A 159, 561 (1970)

# Isvector Giant Resonances

- ▶ In **isovector** giant resonances **neutrons and protons** “oscillate” out of phase  
**e.g.** within a classical picture: “e-m interacting probes basically excite protons, protons drag neutrons thanks to the nuclear strong interaction, when neutrons approach too much to protons, they are pushed out”
- ▶ **Isvector** resonances will depend on oscillations of the density  $\rho_{iv} \equiv \rho_n - \rho_p \Rightarrow S(\rho)$  will drive such “oscillations”
- ▶ The **excitation energy** ( $E_x$ ) within a **Harmonic Oscillator** approach is expected to depend on the symmetry energy:

$$\omega = \sqrt{\frac{1}{m} \frac{d^2U}{dx^2}} \propto \sqrt{k} \rightarrow E_x \sim \sqrt{\frac{\delta^2 e}{\delta \beta^2}} \propto \sqrt{S(\rho)}$$

where  $\beta = (\rho_n - \rho_p)/(\rho_n + \rho_p)$



# Polarizability, Strength distribution and its moments

- ▶ The **linear response** or dynamic polarizability of a **nuclear system excited** from its g.s.,  $|0\rangle$ , to an excited state,  $|\nu\rangle$ , due to the **action of an external isovector oscillating field** (dipolar in our case) of the form  $(F e^{i\omega t} + F^\dagger e^{-i\omega t})$ :

$$F_{JM} = \sum_i^A r^J Y_{JM}(\hat{r}) \tau_z(i) \quad (\Delta L = 1 \rightarrow \text{Dipole})$$

- ▶ is proportional to the **static polarizability** for small oscillations

$$\alpha = (8\pi/9) e^2 m_{-1} = (8\pi/9) e^2 \sum_\nu |\langle \nu | F | 0 \rangle|^2 / E$$

where  $m_{-1}$  is the **inverse energy weighted moment** of the **strength function**, defined as,  $S(E) = \sum_\nu |\langle \nu | F | 0 \rangle|^2 \delta(E - E_\nu)$

- ▶ **Isvector energy weighted sum rules (EWSR)** are:

$$m_1 = \frac{\hbar^2}{2m} \frac{NZ}{A} (1 + \kappa_D) \quad \text{equal to one half of the HF expectation value of } [\hat{F}, [H, \hat{F}]]$$

(Thouless theorem) and where  $\kappa$  is the dipole enhancement factor

# Dipole polarizability: Correlations in EDFs



## Covariance analysis within a model: theory

Given as set of observables  $\mathcal{O}$  used to calibrate the parameters  $\mathbf{p}$  of a given model, the optimum parametrization  $\mathbf{p}_0$  is determined by a fit with the global quality measure,

$$\chi^2(\mathbf{p}) = \sum_{i=1}^m \left( \frac{\mathcal{O}_i^{\text{theo.}} - \mathcal{O}_i^{\text{ref.}}}{\Delta \mathcal{O}_i^{\text{ref.}}} \right)^2$$

Assuming that the  $\chi^2$  is a well behaved (analytical) function in the vicinity of the minimum and that can be approximated by an hyper-parabola,

$$\begin{aligned} \chi^2(\mathbf{p}) - \chi^2(\mathbf{p}_0) &\approx \frac{1}{2} \sum_{i,j}^n (p_i - p_{0i}) \partial_{p_i} \partial_{p_j} \chi^2(p_j - p_{0j}) \\ &\equiv \sum_{i,j}^n (p_i - p_{0i}) \mathcal{M}_{ij} (p_j - p_{0j}) \end{aligned}$$

where  $\mathcal{M}$  is the curvature matrix.

# Dipole polarizability: Correlations in EDFs



## Covariance analysis within a model: theory

$\mathcal{M}$  provides us access to estimate the errors between predicted observables ( $A(\mathbf{p})$ ),

$$\Delta A = \sqrt{\sum_i^n \partial_{p_i} A \varepsilon_{i1} \partial_{p_i} A} \quad (1)$$

$\varepsilon = \mathcal{M}^{-1}$  and the correlations between predicted observables,

$$c_{AB} \equiv \frac{C_{AB}}{\sqrt{C_{AA}C_{BB}}} \quad (2)$$

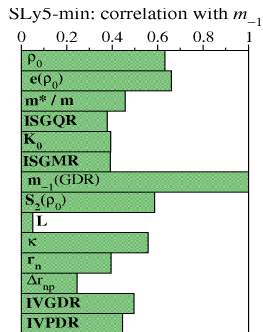
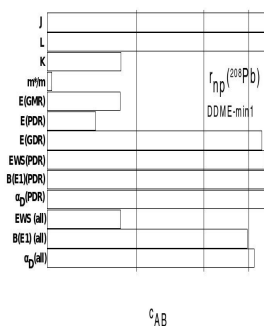
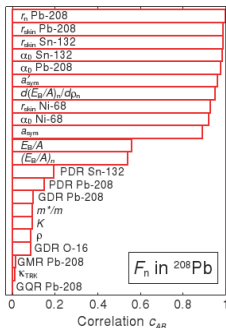
where,

$$C_{AB} = \overline{(A(\mathbf{p}) - \bar{A})(B(\mathbf{p}) - \bar{B})} \approx \sum_{ij}^n \partial_{p_i} A \varepsilon_{ij} \partial_{p_j} B$$

# Dipole polarizability: correlations in EDFs



## Covariance analysis within a model: results



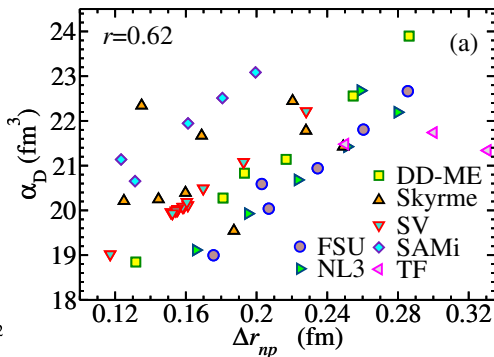
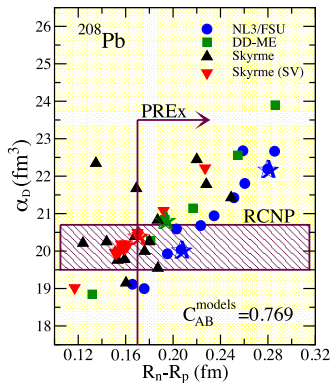
From left to right: SV: P.-G. Reinhard and W. Nazarewicz, Phys. Rev. C 81, 051303(R) (2010); DD-ME1: Nils talk at the INPC 2013; SLy5: X. Roca-Maza

Using the **experimental value**  $\alpha_D = 20.1 \pm 0.6 \text{ fm}^3$  <sup>†</sup> in  $^{208}\text{Pb}$  the **covariance analysis of SV model**, a value  $\Delta r_{np} = 0.156_{-0.021}^{+0.025} \text{ fm}$  was found <sup>†</sup>.

<sup>†</sup> A. Tamii et al., Phys. Rev. Lett. 107, 062502 (2011)

# Dipole polarizability in $^{208}\text{Pb}$ : correlations in EDFs

## Systematics for a set of EDFs



J. Piekarewicz et al., Phys. Rev. C 85, 041302 (2012)

X. Roca-Maza et al., Phys. Rev. C 88, 024316 (2013)

From the models of the left panel, using the **experimental value**  $\alpha_D = 20.1 \pm 0.6 \text{ fm}^3$  <sup>†</sup> in  $^{208}\text{Pb}$  a model average for  $\Delta r_{np} = 0.168 \pm 0.022 \text{ fm}$  was found.

<sup>†</sup> A. Tamii et al., Phys. Rev. Lett. 107, 062502 (2011)

# Dipole polarizability: Correlations in EDFs



## Insights from a macroscopic approach

Given that **only the  $m_{-1}$  moment is required** for the calculation of the **dipole polarizability**, one may perform a constrained calculation

$$\delta \{ \langle \mathcal{H} \rangle - \lambda \langle \mathcal{D} \rangle \} = 0$$

This defines the *constrained energy*  $E(\lambda)$ . **The dielectric theorem** establishes that the  $m_{-1}$  moment may be computed as

$$m_{-1}(E1) = \frac{1}{2} \left. \frac{\partial^2 E(\lambda)}{\partial \lambda^2} \right|_{\lambda=0}$$

Applying **this procedure** in combination with the **droplet model** approach of Myers and Swiatecki<sup>†</sup> yields the following result<sup>††</sup>:

$$\alpha_D = \frac{8\pi}{9} e^2 \frac{A \langle r^2 \rangle}{48J} \left( 1 + \frac{5}{3} \frac{9J}{4Q} A^{-1/3} \right)$$

<sup>†</sup> W. Myers and W. Swiatecki, Annals of Physics 84, 186 (1974)

<sup>††</sup> J. Meyer, P. Quentin, and B. Jennings, Nuclear Physics A 385, 269 (1982)

# Dipole polarizability: Correlations in EDFs



## Insights from a macroscopic approach

Within the DM model:

$$\Delta r_{np} = \sqrt{\frac{3}{5}} \left[ t - \frac{e^2 Z}{70J} \right] + \Delta r_{np}^{\text{surface}}$$
$$t \equiv \frac{3r_0}{2} \frac{J/Q}{1 + \frac{9}{4} \frac{J}{Q} A^{-1/3}} (I - I_C)$$

$Q$  is the so-called surface stiffness coefficient,  $I \equiv (N - Z)/A$  is the relative neutron excess,  $\rho_0 = 3A/4\pi r_0^3$ ,

$I_C = (e^2 Z)/(20JR)$ ,  $R \equiv \sqrt{3/5} r_0 A^{1/3}$ , and  $\Delta r_{np}^{\text{surf}} = \sqrt{3/5} [5(b_n^2 - b_p^2)/(2R)]$  is a correction caused by the difference in the surface width  $b_n$  ( $b_p$ ) of the neutron (proton) density profile

using these expressions:

$$\alpha_D \approx \frac{\pi e^2}{54} \frac{A \langle r^2 \rangle}{J} \left[ 1 + \frac{5 \Delta r_{np} + \sqrt{\frac{3}{5}} \frac{e^2 Z}{70J} - \Delta r_{np}^{\text{surface}}}{\langle r^2 \rangle^{1/2} (I - I_C)} \right]$$

Adopting a value of  $J = 31 \pm 2 \text{ MeV}^\dagger$  one finds for  $^{208}\text{Pb}$  that  $I_C \approx 0.028 \pm 0.002$  ( $\sqrt{3/5}(e^2 Z)/(70J)$  is around  $0.042 \pm 0.003 \text{ fm}$ .  $\Delta r_{np}^{\text{surf}}$  for  $^{208}\text{Pb}$  is almost constant ( $0.09 \pm 0.01 \text{ fm}$ ) in EDFs $^{\dagger\dagger}$

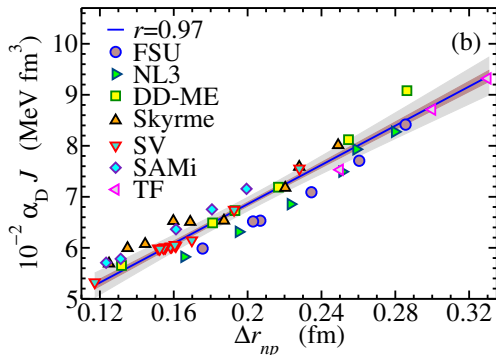
**In the DM  $\Delta r_{np}$  is better correlated with  $\alpha_D J$  than with  $\alpha_D$  alone in a heavy nucleus such as  $^{208}\text{Pb}$**

$^\dagger$  James M. Lattimer, Annu. Rev. Nucl. Part. Sci. 62, 485 (2012)

$^{\dagger\dagger}$  M. Centelles, X. Roca-Maza, X. Viñas, and M. Warda, Phys. Rev. C 82, 054314 (2010).

# Dipole polarizability in $^{208}\text{Pb}$ : Correlations in EDFs

## Insights from a macroscopic approach



X. Roca-Maza et al., Phys. Rev. C 88, 024316 (2013)

Using exp.  $\alpha_D = 20.1 \pm 0.6 \text{ fm}^3$   $^\dagger$  in  $^{208}\text{Pb}$  one finds the relation  
 $\Delta r_{np} = -0.157 \pm (0.002)_{\text{theo.}} + [1.04 \pm (0.03)_{\text{exp.}} \pm (0.04)_{\text{theo.}}] \times 10^{-2} J$

Adopting  $J = 31 \pm (2)_{\text{est.}}$   $\text{MeV}$   $^{\dagger\dagger}$  one obtains

$$\Delta r_{np} = 0.165 \pm (0.009)_{\text{exp.}} \pm (0.013)_{\text{theo.}} \pm (0.021)_{\text{est.}} \text{ fm}$$

$^\dagger$  A. Tamii et al., Phys. Rev. Lett. 107, 062502 (2011)  $^{\dagger\dagger}$  James M. Lattimer, Annu. Rev. Nucl. Part. Sci. 62, 485 (2012)



# Dipole polarizability: Correlations in EDFs



## Insights from a macroscopic approach

Starting from the DM expressions

$$\alpha_D = \frac{8\pi}{9} e^2 \frac{A \langle r^2 \rangle}{48J} \left( 1 + \frac{5}{3} \frac{9J}{4Q} A^{-1/3} \right) \quad \& \quad a_{\text{sym}}(A) = \frac{J}{1 + \frac{9J}{4Q} A^{-1/3}}$$

one can write

$$\alpha_D \approx \frac{8\pi}{9} e^2 \frac{A \langle r^2 \rangle}{48J} \left( 1 + \frac{5}{3} \frac{J - a_{\text{sym}}(A)}{J} \right)$$

and assuming that the **symmetry energy coefficient of a finite nucleus is very close to that of the infinite system**<sup>†</sup> at an **appropriate** sub-saturation density  $\rho_A$ :  $a_{\text{sym}}(A) \approx S(\rho_A)$ :

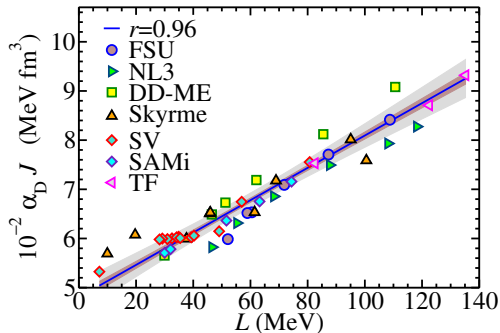
$$\alpha_D \approx \frac{\pi e^2}{54} \frac{A \langle r^2 \rangle}{J} \left[ 1 + \frac{5}{3} \frac{L}{J} \epsilon_A \right]$$

where  $\epsilon_A \equiv \frac{\rho_0 - \rho_A}{3\rho_0}$  and  $\epsilon_{208} = 1/8$  for  $\rho_0 = 0.16 \text{ fm}^{-3}$  for the case of  $^{208}\text{Pb}$

<sup>†</sup>M. Centelles, X. Roca-Maza, X. Viñas, and M. Warda, Phys. Rev. Lett. 102, 122502 (2009)

# Dipole polarizability in $^{208}\text{Pb}$ : Correlations in EDFs

## Insights from a macroscopic approach



X. Roca-Maza et al., Phys. Rev. C 88, 024316 (2013)

Using exp.  $\alpha_D = 20.1 \pm 0.6 \text{ fm}^3$   $^\dagger$  in  $^{208}\text{Pb}$  one finds the relation

$$L = -146 \pm (1)_{\text{theo.}} + [6.11 \pm (0.18)_{\text{exp.}} \pm (0.26)_{\text{theo.}}] J$$

Adopting  $J = 31 \pm (2)_{\text{est.}}$   $\text{MeV}$   $^\dagger\dagger$  one obtains

$$L = 43 \pm (6)_{\text{exp.}} \pm (8)_{\text{theo.}} \pm (12)_{\text{est.}} \text{ MeV}$$

$^\dagger$  A. Tamii et al., Phys. Rev. Lett. 107, 062502 (2011)  $^\dagger\dagger$  James M. Lattimer, Annu. Rev. Nucl. Part. Sci. 62, 485 (2012)

# Dipole polarizability in exotic nuclei

**SCRIT: a unique experimental tool for the study of fundamental properties of exotic nuclei<sup>†</sup>**

- ▶ The **e-m charge distribution of unstable Sn (Z=50) isotopes** will be measured at the **SCRIT (RIKEN) facility next year via electron elastic scattering**.
- ▶ If measuring the **E1** response from inelastic electrons at forward angles **becomes feasible using SCRIT<sup>††</sup>**, the **neutron skin of exotic nuclei** and **L** might be **extracted experimentally from the same facility** using the correlation between  **$\alpha_D J$  and  $\Delta r_{np}$** .

<sup>†</sup> [http://www.riken.jp/en/research/labs/rnc/instrum\\_dev/scrif/](http://www.riken.jp/en/research/labs/rnc/instrum_dev/scrif/)

<sup>††</sup> T. Suda et al. Prog. Theor. Exp. Phys. 2012, 03C008



# CONCLUSIONS

# Conclusions:

## For medium-heavy and heavy mass nuclei we expect:

- ▶ the **macroscopic model** presented here contains **relevant physics** for the description of the **dipole polarizability**

(accurate within a 10% when compared with self-consistent calculations)

- ▶  $\alpha_D J$  is strongly correlated with the  $\Delta r_{np}$  and  $L$  in EDFs.

## For the case of $^{208}\text{Pb}$ with exp. value $\alpha_D = 20.1 \pm 0.6 \text{ fm}^3$ :

- ▶  $\Delta r_{np} = -0.157 \pm (0.002)_{\text{th.}} + [1.04 \pm (0.03)_{\text{exp.}} \pm (0.04)_{\text{th.}}] 10^{-2} \text{ J}$
- ▶  $L = -146 \pm (1)_{\text{theo.}} + [6.11 \pm (0.18)_{\text{exp.}} \pm (0.26)_{\text{theo.}}] \text{ J}$

## ... and assuming $J = 31 \pm (2)_{\text{est}} \text{ MeV}$ :

- ▶  $\Delta r_{np} = 0.165 \pm (0.009)_{\text{exp.}} \pm (0.013)_{\text{theo.}} \pm (0.021)_{\text{est.}} \text{ fm}$
- ▶  $L = 43 \pm (6)_{\text{exp.}} \pm (8)_{\text{theo.}} \pm (12)_{\text{est.}} \text{ MeV}$

## Co-workers:

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